



# Phase Equilibrium Data Correlation



## ✓ Examples of objective functions

$$O.F._{total} = O.F._{x,LL} + O.F._{x,LLL} + O.F._{y,LV} + \dots$$

$$O.F._{x,L_1L_2} = \sum_{j=1}^{NTL} \sum_{q=1}^2 \sum_{i=1}^C \left( x_{i,j}^{Lq,exp} - x_{i,j}^{Lq,cal} \right)^2$$

subject to:

$$\left\{ \sum_{j=1}^{NTL} \sum_{i=1}^C \left( a_{i,j}^{L1,cal} - a_{i,j}^{L2,cal} \right)^2 < \varepsilon \dots \right.$$

$$O.F._{x,L_1L_2L_3} = \sum_{k=1}^3 \sum_{i=1}^C \left( x_i^{Lk,exp} - x_i^{Lk,cal} \right)^2$$

subject to:

$$\left\{ \sum_{p=1}^2 \sum_{k>p}^3 \sum_{i=1}^C \left( a_i^{Lp,cal} - a_i^{Lk,cal} \right)^2 < \varepsilon \dots \right.$$

$$O.F._{y,LV} = \left\{ \begin{array}{l} \sum_{j=1}^{NTL} \sum_{i=1}^C \left( y_{i,j}^{exp} - y_{i,j}^{cal} \right)^2 \\ \sum_{j=1}^{NTL} \sum_{i=1}^C \left( T_{i,j}^{exp} - T_{i,j}^{cal} \right)^2 \\ \sum_{j=1}^{NTL} \sum_{i=1}^C \left( g_{i,j}^{ML,exp} - g_{i,j}^{ML,cal} \right)^2 \\ \sum_{j=1}^{NTL} \sum_{i=1}^C \left( \frac{\gamma_{i,j}^{exp} - \gamma_{i,j}^{cal}}{\gamma_{i,j}^{exp}} \right)^2 \dots \end{array} \right.$$

subject to:

$$\left\{ \begin{array}{l} \sum_{j=1}^{NTL} \left( \sum_{i=1}^C y_{i,j}^{cal} - 1 \right)^2 < \varepsilon \\ \sum_{j=1}^{NTL} \sum_{i=1}^{C-1} \left( \frac{\partial g_j^{M,V}}{\partial y_{i,j}^{cal}} - \frac{\partial g_j^{M,L}}{\partial x_{i,j}^{exp}} \right)^2 < \varepsilon \dots \end{array} \right.$$

j = Tie lines (1, ..., NTL)

i = Components (1, ..., C)

q = Liquid phases of a LLE tie lines (e.g. L<sub>1</sub>L<sub>2</sub>)

k,p = Liquid phases of a LLE tie triangle (e.g.: L<sub>1</sub>, L<sub>2</sub> and L<sub>3</sub>)



# Examples of data correlation analysis & procedures



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# Examples of correlation data analysis & procedures



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