ORIGINAL ARTICLE



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# On the consistency of the current conventional EOP series and the celestial and terrestrial reference frames

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Abstract Precise transformation between the celestial ref-1 erence frames (CRF) and terrestrial reference frames (TRF) 2 is needed for many purposes in Earth and space sci-3 ences. According to the Global Geodetic Observing System Δ (GGOS) recommendations, the accuracy of positions and sta-5 bility of reference frames should reach 1 mm and 0.1 mm year $^{-1}$ , and thus, the Earth Orientation Parameters (EOP) should be estimated with similar accuracy. Different real-8 izations of TRFs, based on the combination of solutions from four different space geodetic techniques, and CRFs, 10 based on a single technique only (VLBI, Very Long Base-11 line Interferometry), might cause a slow degradation of the 12 consistency among EOP, CRFs, and TRFs (e.g., because of 13 differences in geometry, orientation and scale) and a mis-14 alignment of the current conventional EOP series, IERS 08 15 C04. We empirically assess the consistency among the con-16 ventional reference frames and EOP by analyzing the record 17 of VLBI sessions since 1990 with varied settings to reflect 18 the impact of changing frames or other processing strategies 19 on the EOP estimates. Our tests show that the EOP estimates 20 are insensitive to CRF changes, but sensitive to TRF varia-21 tions and unmodeled geophysical signals at the GGOS level. 22 The differences between the conventional IERS 08 C04 and 23 other EOP series computed with distinct TRF settings exhibit 24 biases and even non-negligible trends in the cases where no 25 differential rotations should appear, e.g., a drift of about 20 26

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μas year1 in ypolwhen the VLBI-only frame VTRF2008 is27used. Likewise, different strategies on station position mod-<br/>eling originate scatters larger than 150 μas in the terrestrial28pole coordinates.30

**Keywords** Earth orientation parameters · Reference systems · Reference frames · VLBI

# **1** Introduction

Assessing the actual accuracy of the earth orientation para-34 meters (EOP) is still an open and timely question, into which 35 we need more insight in view of the demanding requirements 36 of accuracy and stability pursued at present by, e.g., GGOS, 37 the Global Geodetic Observing System of the International 38 Association of Geodesy (IAG)-Plag and Pearlman (2009). 39 GGOS goals are 1 mm in accuracy and 0.1 mm/year in sta-40 bility of the reference frames; those values, when measured 41 on the Earth surface, correspond, respectively, to just above 42 30  $\mu$ as and 3  $\mu$ as/year in terms of angles from the Earth's 43 centre, or 2  $\mu$ s and 0.2  $\mu$ s/year in time units, and they were 44 adopted by the IAU/IAG Joint Working Group on Theory 45 of Earth Rotation (Ferrándiz and Gross 2014). Operational 46 EOP are provided for worldwide use by the Earth Orienta-47 tion Centre (EOC) of the International Earth Rotation and 48 Reference System Service (IERS); IERS also hosts for the 49 product centers: the conventional International Celestial and 50 Terrestrial Reference Frames (ICRF and ITRF, respectively). 51 According to the IERS Conventions (2010) (Petit and Luzum 52 2010), the conventional daily EOP are currently realized by 53 the time series IERS 08 C04 that links the conventional real-54 ization of the ICRS, currently ICRF2 (Fey et al. 2015) to 55 the conventional realization of the ITRS denoted ITRF2008 56 (Altamimi et al. 2011). 57

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The computation of the ITRF depends on a complex

process, in which the solutions produced by the four main

space geodetic techniques and by various analysis centers

(AC) are combined. Regarding input data, it is assumed

that each technique refers to its own reference system and,

furthermore, each coordinate epoch refers to a separate

reference system (Altamimi et al. 2011). The stacking is per-

formed in two steps, the first is applied to data from each

single technique separately and the second brings the former

results together to derive a common ITRF. The concurrence

of all those factors is a source of intricacies and makes dif-

ficult the assessment of the actual accuracy of the EOP. In

any case, the solutions for EOP and ITRF are obtained, so

that they provide optimal consistency among them, accord-

ing to certain optimality criteria that involve the least-squares

minimization of unknown parameters or apparent coordi-

nate variations as described in detail, e.g., in Altamimi and

Dermanis (2012). However, whereas the nature of an ITRF

compels it to last for some years and be "frozen" during a cer-

tain period before the release of the next reference frame, the

EOP must be provided on a more continuous basis. The IERS

08 C04 conventional EOP series are also produced under a

combination process that consists of several steps and gathers

data from all techniques. It is detailed in Bizouard and Gam-

bis (2011). This combination process is unconnected to the

ITRF combination, in the sense that the EOP solution is not

forced to coincide with the solution computed along with the

ITRF in their common time span, but it is computed from the

technique-wise EOP solutions imposing certain constraints,

as for instance, the absence of trends w.r.t. the ITRF2008.

Of course, neither the accuracy nor the consistency between

the EOP determined from data beyond the time interval used

in the realization of the reference frames, and those frames

themselves can be ensured a priori and must be estimated

a posteriori. It is clear than the accuracy of the resulting

EOP solution cannot surpass that of the implied frames, but

could be worse. In this complex situation, accuracy is usually

estimated in terms of formal errors, uncertainties, or repeata-

bility, and the assessment of the actual (not the assumed)

accuracy of the current conventional EOP becomes a cumber-

some issue, though tightly linked to the level of consistency

mutual consistency of the time series IERS 08 C04 together

with ITRF2008 and ICRF2, not restricted to the time interval

used for the frame building. The procedure relies on perform-

ing suitable analysis of observational data. We follow the

standard ideas used in the validation of empirical models,

which requires analyzing the residuals between models and

observations, irrespective of the simplicity or complexity of

the model. It seems reasonable that the first step should be

the analysis of VLBI data, since VLBI is the only technique

capable of providing operative solutions for the whole set of

The objective of this article is to investigate the issue of the

between the IERS 08 C04 series, ITRF2008, and ICRF2.

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EOP. The analysis could provide more insight not only into<br/>accuracy or consistency issues, but also into the features of<br/>VLBI solutions compared with combined solutions and into<br/>the current limits of model improvement.111112113

Our analyses comprise all the VLBI sessions between 115 1990 and 2013. The EOP are derived in the form of time 116 series similar to the conventional ones, each one correspond-117 ing to distinct changes in the processing settings which are 118 explained in detail in Sects. 2 and 3. Section 3 comprises 119 several subsections, each one covering a test problem empir-120 ically. In the first subsection, we present the results of an 121 experiment designed to assess the effect of unrestricted, 122 unmodeled geophysical signals on the EOP series. Next, the 123 sensitivity of the VLBI EOP solutions to the change of the 124 a priori EOP series is addressed. In Sects. 3.3 and 3.4, we 125 test some TRF and CRF realizations (distinct from those 126 used in the IERS 08 C04 derivation) to study their impact 127 on the EOP, especially in the long-term, paying attention to 128 the appearance of biases and especially trends among the 129 different EOP series, which would suggest the emergence 130 of differential rotations. The last Sect. 3.5 aims at discern-131 ing to which extent the behaviour found in Sect. 3.3 can be 132 attributed to differential orientations of the TRFs. Finally, 133 in Sect. 4, the main points of the former individual exper-134 iments are summarized and discussed, and the conclusions 135 are drawn. 136

The results in this article are an extension and continuation 137 of our previous results contained in two conference papers 138 by Heinkelmann et al. (2014b, 2015). Those papers intro-139 duce the basic ideas and methodology in a concise way and 140 emphasize on the interpretation of the results and the discus-141 sion of the consistency among frames rather than on EOP. 142 In those previous analyses, all the VLBI sessions since 1984 143 were accounted for. Here, we decided to remove them from 144 the analysis as recommended by different authors (Malkin 145 2013b; Chao and Hsieh 2015), in view of the small magnitude 146 of the effects found in the first analysis and the inaccuracy 147 of data in the earlier years. In this case, the modification of 148 the analysis period does not produce substantial qualitative 149 changes, apart from the differences in the numerical results 150 displayed in Table 3 here and Table 1 in Heinkelmann et al. 151 (2015). Sections 3.2 and 3.5 do not have a counterpart in the 152 precedent studies. 153

#### 2 Data analysis

The consistency issues are assessed by performing different VLBI data analyses, which are extended to 2912 sessions ranging from 1990-01-18 until 2013-12-31 (GFZ VLBI contribution to ITRF2013; Heinkelmann et al. 2014a); the initial years until 1990 have been excluded from the analysis due to the lower quality of the VLBI data. The GFZ version 1600

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of the Vienna VLBI software (VieVS, Böhm et al. 2012), 161 VieVS@GFZ, was utilized, with the following common 162 processing options: for each EOP, one offset per day with 163 respect to a selected a priori series (usually IERS 08 C04) 164 was estimated for each VLBI session. For modeling, the 165 tropospheric delays we used the Vienna mapping functions 166 (VMF1, Böhm et al. 2006), and we estimated the zenith wet 167 delays and the tropospheric gradients as piece-wise linear 168 functions with 1 h and 6 h interval lengths, respectively. The 169 station clock offsets were estimated as piece-wise linear func-170 tions with 1 h interval lengths, plus quadratic terms (Nilsson 171 et al. 2014). After single-session adjustments, we discarded 172 about 50 VLBI sessions with a posteriori sigma of unit weight 173 larger than 3. 174

Other processing options depend on the different analy-175 ses that have been performed and will be detailed in the 176 corresponding sections. For instance, when we intended to determine the effect of a specific TRF or CRF on the EOP, 178 we fixed the station and source coordinates on their cat-179 alogue values. Thus, various EOP series were determined 180 using different celestial (Table 1) and terrestrial (Table 2) reference frames for computing each solution and varying the a priori EOP series (IERS 08 C04, USNO finals, and IAU 183 2000/2006 precession-nutation models). When the aforementioned products are evaluated using VLBI data only, 185 it should be remarked that the assessment would show the 186 (in)consistency among the products with respect to VLBI data, but the results should not be extrapolated to other techniques.

To compare the different pairs of EOP time series estimates, we calculated the Weighted Mean (WM) of the

Table 1 Different CRFs used in this study

CRF	References	Comment
ICRF-Ext.2	Ma et al. (1998)	Orientation is based on data until 1995.5
	Fey et al. (2004)	
ICRF2	Ma (2009)	Data until (2009)
	Fey et al. (2015)	

Table 2 Different TRFs used in this study

differences and the Weighted Root Mean Square (WRMS) 102 differences between each of them, by means of the following 193 formulae (Nilsson et al. 2014), where sub-indices eop1 and 194 eop2 denote the individual solution: 195

$$WM = \frac{\sum_{i=1}^{N} \frac{\tilde{x}_{\text{cop1},i} - \tilde{x}_{\text{cop2},i}}{\sigma_{\text{cop1},i}^2 + \sigma_{\text{cop2},i}^2}}{\sum_{i=1}^{N} \frac{1}{\sigma_{\text{cop1},i}^2 + \sigma_{\text{cop2},i}^2}}$$
(1) 196

WRMS = 
$$\sqrt{\frac{\sum_{i=1}^{N} \frac{(\tilde{x}_{\text{copl},i} - \tilde{x}_{\text{cop2},i} - \text{WM})^2}{\sigma_{\text{cop1},i}^2 + \sigma_{\text{cop2},i}^2}}{\sum_{i=1}^{N} \frac{1}{\sigma_{\text{cop1},i}^2 + \sigma_{\text{cop2},i}^2}}}$$
 (2) 197

where,  $\tilde{x}$  denote the estimates of EOP values from the VLBI 198 analysis using the different settings, N their number and 199  $\sigma$  indicate their respective formal uncertainties. Moreover, 200 when analyzing the residuals between a pair of different EOP 201 solutions, a linear trend was computed, composed of a shift 202 (referred to epoch J2000.0) and a linear drift calculated by 203 Least Squares (LS) or Weighted Least Squares (WLS), where 204 the error of fits was assessed by the weighted root mean 205 square (denoted by WRMS). 206

Suitable statistical tests were also applied to ensure that 207 the results are statistically significant at the 0.05 level ( $\alpha$ ) 208 before drawing conclusions. Since the series are normally 209 distributed, the WM values were analyzed by t test and the 210 WRMS values by F test. 211

#### **3 Results**

#### 3.1 Unmodeled geophysical signals

The first analysis is concerned with the effect of unmodeled 214 geophysical signals affecting the position of VLBI stations. 215 Notice that unmodeled is used in the proper sense of a com-216 ponent of a signal not accounted in a given model adopted 217 in the processing strategy, it should not be understood neces-218 sarily as a deficiency of a conventional model. Let us recall 219 that the determined station coordinates do not have a simple 220 dependency on geophysical signals, since several models rec-221

TRF	Reference	Comment
ITRF2000	Altamimi et al. (2002)	Data until 2000
ITRF2005	Altamimi et al. (2007)	Data until 2005
ITRF2008	Altamimi et al. (2011)	Data until 2008
VTRF2008	Böckmann et al. (2010)	Data until 2008, VLBI-only frame, contains the same VLBI data as it was provided to ITRF2008 and DTRF2008
DTRF2008	Seitz et al. (2012)	Data until 2008, contains the same data as ITRF2008, but using a different combination approach

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ommended in the IERS Conventions (i.e., solid Earth tides, 222 oceanic, and atmospheric tidal loading) are applied as a priori 223 models in various data analyses, including the TRF esti-224 mation. However, other geophysical effects (i.e., non-tidal 225 atmosphere, non-tidal ocean, and hydrological loading) are not recommended for the conventional analyses; their effect on the results is accumulated together with the inaccuracies of the considered a priori models. Besides, the adopted model for the station coordinates is linear, made up of a position and a constant velocity. The consequence of all that is that the appearance of unmodeled geophysical signals may propagate into inaccuracies of the EOP.

That possibility was clearly confirmed in a recent paper by Krásná et al. (2015). They estimated three different VLBI solutions to evaluate the impact of the unmodeled seasonal 237 signals in the station displacement on the CRF and EOP. In the first solution, the seasonal displacement was omitted 238 (reference signal). In the second alternative harmonic cor-239 rections, composed of annual and semi-annual constituents, 240 they were computed for a number of stations and used to 241 improve the model of their displacements. In addition, in the 242 third option, the seasonal displacement was modeled with a 243 mean annual model, which had been described and applied 244 by Tesmer et al. (2009). With this analysis, Krásná et al. 245 (2015) unveiled the existence of differences of several tens 246 of µas into the ERP determinations, as well as large drifts 247 (1.82  $\mu$ as year<sup>-1</sup> in y<sub>pol</sub> and -0.10  $\mu$ s year<sup>-1</sup> in dUT1) 248 when VieTRF13b and VieCRF13b (Krásná et al. 2014) were 249 used as a priori reference frames together with the harmonic 250 model. These results agree with the previous studies per-251 formed by Ding et al. (2005), Tesmer et al. (2009), Malkin 252 (2013a), and Eriksson and MacMillan (2014), who found 253 unmodeled annual and semi-annual displacements in the sta-254 tion horizontal coordinates. Let us recall that the current 255 conventional standards for the station motions only account 256 for a constant velocity term-although they will be extended 257 in the next TRF realization, ITRF2014. For these model 258 limitations and to avoid damaging effects, fixing station coor-259 dinates to their a priori values is not recommended by the 260 scientific community, in general, and in particular when esti-261 mating EOP. 262

In this test, we neither determine nor apply seasonal com-263 ponents to correct the station positions, since we aim at 264 assessing the uncertainty and stability of the current con-265 ventional products (ITRF2008, ICRF2, and IERS 08 C04), 266 attributable to any kind of unmodeled geophysical signal 267 (seasonal or not) affecting the regularized station coordinates 268 reported in the ITRF2008 catalogue. We proceed by estimat-269 ing the EOP through two different approaches: 270

(a) FIXED ITRF2008 coordinates (unmodeled geophysical 271 signals propagate into EOP). 272

(b) FREE ITRF2008 coordinates (unmodeled geophysical 273 signals cause adjustments of station coordinates). This 274 means that the positions and velocities of all station coor-275 dinates were estimated by imposing no-net-translation 276 and no-net-rotation conditions with respect to ITRF2008. 277

For numerical assessment, we compare the resulting EOP 278 series (approach a vs. b) to quantify how important the effects 279 of the unmodeled geophysical signals are. The first global 280 indicators of the differences are provided by the mean and 281 the dispersion of the differences of the series computed for 282 each EOP. Table 3 displays the WM and WRMS differences 283 between the two solutions and shows the shifts and drifts of 284 the EOP differences w.r.t. IERS 08 C04 and the correlations 285 among the two approaches. Fixing station positions to their 286 nominal values in the ITRF2008 catalogue causes no statis-287 tically significant (p value > 0.05) WM differences of all 288 EOP; however, it generates noticeable scatter between both 289 solutions, that reaches about 144, 164, and 5.9 µs for the 290 differences in  $x_{pol}$ ,  $y_{pol}$ , and dUT1, respectively. 291

The celestial pole offsets (CPO) are insignificantly affected 292 by unmodeled signals: the correlation coefficients between 203 solutions following approach a and approach b are very large 294 (0.95 and 0.94), and their WRMS are not significant (p value 295 > 0.05) affected by the approach (Table 2). However, we 296 notice a small shift of 15 µas and a drift at the level of 3 297  $\mu$ as/year of the Y component of the CPO in both approaches; 298 that value is at the limit of the GGOS stability goal. That 299 drift is nearly the same found in our previous work, includ-300 ing the VLBI sessions since 1984, but in that case, there also 301 appeared a shift of dUT1 with a magnitude of 5.7  $\mu$ s, much 302 larger than the shifts displayed in Table 3, at the level of 4.5 303  $\mu$ s for dUT1. The 4.5  $\mu$ s shift for dUT1 is significantly larger 304 than the GGOS goal. If the results are compared with Table 305 1 in Heinkelmann et al. (2015), which covers 1984–2013, 306 there is a pattern common to all the EOPs, namely very close 307 drifts and different biases. 308

Concerning Table 3 it is important to note that the dif-309 ferent handling of the TRF station coordinates (fixed and 310 free approach) results in a strong decrease of the correla-311 tion between each series of Earth Rotation Parameters (ERP) 312 strategy as a consequence of the neglected signals, which 313 happens to be close to 50 % in the case of the pole coordi-314 nates and is consistent with the large values of the WRMS 315 shown in the last column of Table 3, with an average near 150 316 μas. That large scatter is about five times the GGOS accuracy 317 target, what confirms that the modeling of the station position 318 is one of the key problems to improve the EOP repeatability. 319 Besides, the WRMS (weighted root mean square after sub-320 tracting the linear component of the difference) of the ERP 321 especially increase from the fixed to the free approach; our 322 explanation for this fact is that the IERS 08 C04 EOP are 323 consistent with the linear station model of ITRF2008, and 324

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EOP	ITRF2008 fixed	p		ITRF2008 free			FIXED VS IFEE						
	Shift	Drift	WRMS	Shift	Drift	WRMS	Shift	Drift	Amplitude		Corr	Corr WM	WRMS
									Annual	Semi-annual			
$\Delta x_{\rm pol}(\mu  {\rm as})$	$-17.5 \pm 8.2$	$-2.4 \pm 0.5$ 130.9	130.9	$-28.3 \pm 10.8$	$-2.4\pm0.6$	173.9	$6.9\pm8.3$	$0.5\pm0.5$	$14.5 \pm 3.9$	$11.2 \pm 3.9$ 0.55	0.55	10.1	144.0
$\Delta y_{\rm pol}(\mu  {\rm as})$	$-0.02\pm7.2$	$1.2\pm0.5$	120.3	$-33.7\pm11.5$	$4.0\pm0.6$	181.8	$26.9\pm10.1$	$-2.1\pm0.6$	$11.7 \pm 4.5$	$2.3 \pm 4.4$	0.45	15.3	164.3
$\Delta dUT1(\mu s)$	$4.5\pm0.5$	$-0.2\pm0.03$	8.1	$4.8\pm0.6$	$-0.2\pm0.03$	10.1	$-0.3\pm0.3$	$-0.01\pm0.02$	$0.49 \pm 0.1$	$0.10\pm0.1$	0.68	-0.4	5.9
$\Delta X(\mu as)$	$-2.2 \pm 4.4$	$-2.2 \pm 4.4$ $0.8 \pm 0.2$	77.2	$-0.3 \pm 4.4$	$0.6\pm0.2$	78.2	$-2.0\pm1.1$	$0.2\pm0.1$	$1.3 \pm 0.5$	$1.2\pm0.5$	0.95	-0.7	19.6
$\Delta Y(\mu as)$	$15.9 \pm 4.5$	$-3.3 \pm 0.3$	78.5	$16.6\pm4.6$	$-3.4\pm0.2$	79.2	$-0.5\pm1.1$	$0.1\pm0.1$	$1.6\pm0.5$	$0.8\pm0.5$	0.94	-0.3	19.7

consequently, if station coordinates differ from their cata-325 logue value, the EOP scatter will increase. Figure 1 displays 326 the ERP differences w.r.t. IERS 08 C04 for the fixed and free 327 approaches to help to graphically decipher the time scales 328 present in the large differences and reduced correlations. 329 As noted by Krásná et al. (2015), the main discrepancies 330 present a dominant annual pattern. However, these differ-331 ences cannot be only modeled with annual and semi-annual 332 constituents, since they are composed of more complex sig-333 nals. This fact can be seen in the periodograms of the ERP 334 differences between both approaches (Fig. 2). Regarding the 335 pole coordinates, the maximal spectral power is located near 336 the 1 year period, heterogeneous patterns of higher frequen-337 cies being visible too. Their provenance is unclear, but some 338 of them may have actual physical origin. In any case, we have 339 fitted annual and semi-annual harmonic constituents to each 340 EOP and show the results also in Table 3, to compare them to 34 Krasna's et al. results. The orders of magnitude are similar, 342 which provides additional evidence on the consistency level. 343 Our values are closer to their S3–S1 difference in Table 8, 344 which do not use harmonic models for the seasonal station 345 positions but non-linear annual means. That fact suggest that 346 the use of a harmonic model for the station position varia-347 tions may have more significant impact on EOP than using 348 smoother or no models, although more insight in the issue is 349 needed to draw a conclusion. 350

# 3.2 Different a priori EOP series

In an ideal case, the estimated values of the EOP should be the 352 same independent of the a priori values. However, the highly 353 accurate estimation of the full set of EOP is not simple from 354 either a mathematical or physical perspective, and the possi-355 bility of having effects derived from the choice of the initial 356 solution should be investigated. In this test, several a priori 357 EOP series were used to estimate the EOP by VLBI fixing 358 the reference frames to the current conventional ITRF2008 359 and ICRF2. First, VLBI time series were determined using a 360 priori EOP from IERS 08 C04 (case 1), second, the a pri-36 ori ERP and Celestial Pole Coordinates were taken from 362 IERS 08 C04 and from the IAU 2006/2000A precession-363 nutation model, respectively (case 2), and finally, the USNO 364 Finals time series were used as a priori EOP values (case 365 3). The comparison shows no significant (p value > 0.05) 366 EOP WM differences between the IERS 08 C04 and USNO 367 Finals approaches (cases 3 vs 1), whereas their repeatabili-368 ties (measured by the WRMS) are close to 40  $\mu$  as in all the 369 EOP with the exception of dUT1 that is around 5.3 µs, i.e., 370 more than 2.5 times the corresponding GGOS accuracy of 371  $2 \mu s$  (Fig. 3). EOP residuals reveal almost negligible shifts 372 and drifts (Table 4). Therefore, VLBI-determined EOP using 373 either IERS 08 C04 or USNO Finals as a priori values are in 374 a very good agreement (correlation about 0.93). 375

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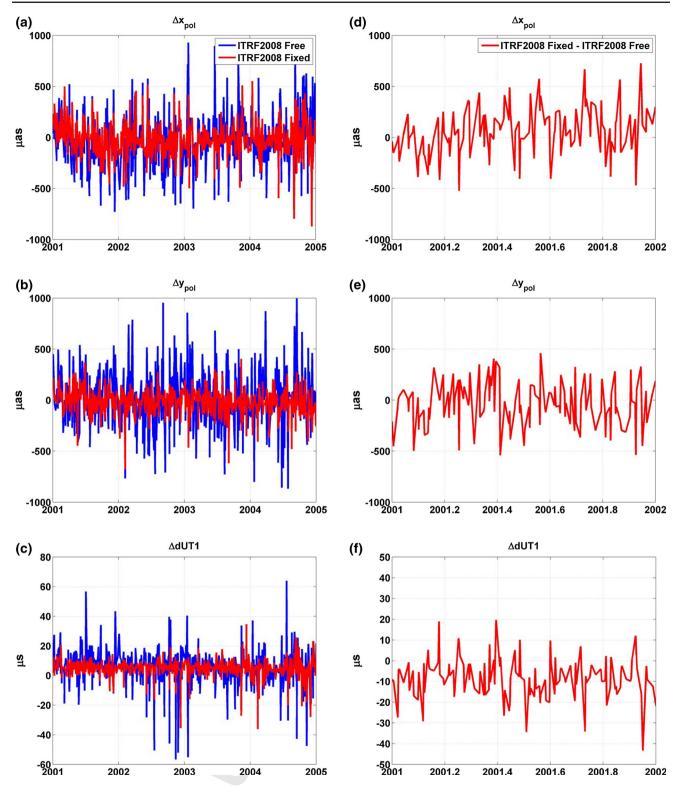


Fig. 1 ERP residuals w.r.t. IERS 08 C04 between solutions using fixed (*red line*) and free (*blue line*) ITRF2008 coordinates observed from 2001 to 2005 (*left column*). Differences between both solutions zoomed-in from 2001 to 2002 (*right column*). Units µas or µs for dUT1

The interpretation of the differences between the cases 1 and 2 is not so simple (Fig. 3). First, the WM differences of the polar motion (PM) parameters and dUT1 are insignificant (*p*  value > 0.05), as it could be expected, since the a priori values for the three ERP were not changed. It is important to remark that the WM results correlate strongly with the shifts listed in 381

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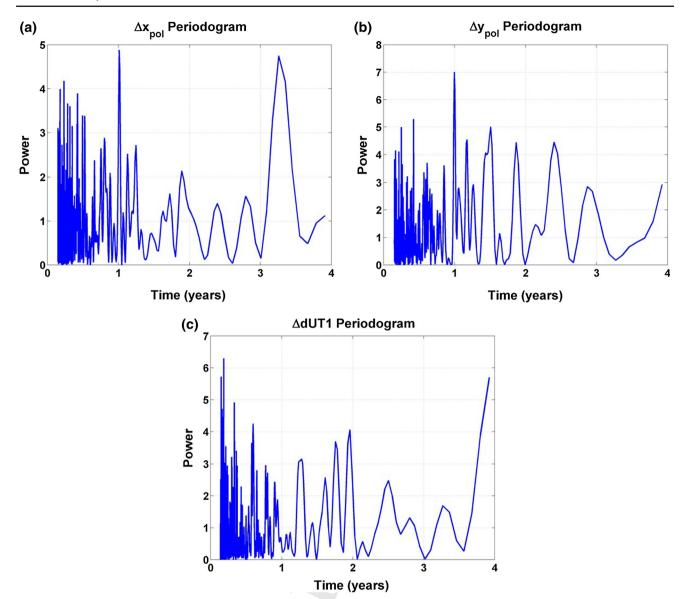
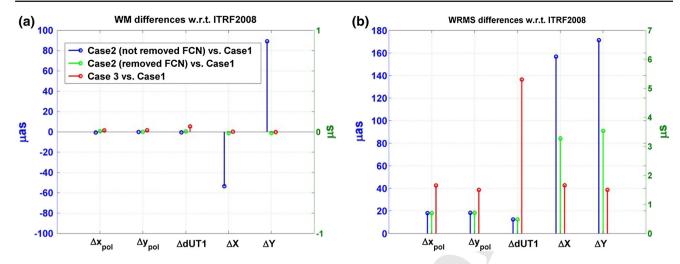


Fig. 2 Periodograms of the differences between ERP estimated by different approaches: fixed and free ITRF2008 coordinates. A priori EOP series: **IERS 08 C04** 

Table 4. As for the WRMS values, in contrast to the precedent 382 case, they are about 20 µas for both PM components and 383 smaller for dUT1. The differences between the CPO are much 384 more significant (p value < 0.05), as expected, since they 385 correspond roughly to the deviation between the conventional 386 nutation theory and the operational solution. It is known that 387 the IAU-adopted precession/nutation model, currently IAU 388 2006/2000A (Dehant 2002; Hilton et al. 2006), contains only 389 the easier to predict, forced astronomical effects, and thus, 390 the Free Core Nutation (FCN) is not included. This has a 391 powerful impact on the residuals-apart from the need of some additional corrections. Besides WRMS over 160 µas, 393 we detect statistically significant WM differences ( $-55 \mu as$ 394 in dX and 93  $\mu$ as in dY) and large shifts (-39.8  $\mu$ as in dX 395

and 94.2  $\mu$  as in dY) (Table 4) of the CPO between the IERS 396 08 C04 and IAU 2006/2000A approaches with a significance 397 level 0.05, showing considerable scattering (WRMS of about 398 160 µas). The importance of using a good FCN model to get 399 smaller residuals is well known. Nowadays, several empirical 400 models are available with high temporal resolution and accu-401 racy (Lambert 2007; Malkin 2010, 2013b; Krásná et al. 2013; 402 Belda et al. 2016). We modify the case 2 by adding to IAU 403 2006/2000A the model determined recently by Belda et al. 404 (2016), which was fitted to VLBI data using a sliding window 405 length of 400 days displaced 1 day and a constant period of 406 -431.18 sidereal days for the signal, so that we can remove 407 the FCN oscillations that appear in case 2 (Fig. 4). To study 408 the remaining residuals ( $[\Delta X, \Delta Y] = CPO - FCN$ ), the 409

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**Fig. 3** WM and WRMS differences between EOP estimated with different a priori EOP. *Case 1* EOP  $\rightarrow$  IERS 08 C04. *Case 2* ERP  $\rightarrow$  IERS 08 C04 and *X*, *Y*  $\rightarrow$  IAU 2006/2000A. *Case 3* EOP  $\rightarrow$  USNO Finals. Units: µas (*left side*) or µs (*right side*) for dUT1

Table 4EOP Differences ( $\mu$  asor  $\mu$ s for dUT1) betweensolutions using different a prioriEOP series

EOP	Case 2 vs. case	1		Case 3 vs. case	e 1	
	Shift	Drift	WRMS	Shift	Drift	WRMS
$\Delta x_{\rm pol}~(\mu as)$	$-0.9 \pm 1.1$	$0.0 \pm 0.1$	18.1	$-0.9\pm2.7$	$-0.1\pm0.2$	42.6
$\Delta y_{\text{pol}}$ (µas)	$-0.7\pm1.1$	$0.1 \pm 0.1$	18.4	$-2.4\pm2.3$	$0.2\pm0.1$	38.7
$\Delta dUT1 \ (\mu s)$	$0.0\pm0.03$	$0.0 \pm 0.01$	0.5	$0.0\pm0.02$	$0.0\pm0.02$	5.3
$\Delta X$ (µas)	$-39.8\pm8.9$	$-2.5\pm0.5$	156.2	$0.7\pm2.4$	$-0.2\pm0.1$	42.8
$\Delta Y$ (µas)	$94.2\pm9.9$	$-0.9\pm0.6$	171.3	$-0.3\pm2.2$	$0.1\pm0.1$	38.7

Shift (referred at epoch J2000.0) and linear trends (year<sup>-1</sup>) are estimated by WLS. The WRMS are computed after subtracting the linear component of the difference *Case 1* EOP  $\rightarrow$  IERS 08 C04. *Case 2* ERP  $\rightarrow$  IERS 08 C04 and *X*, *Y*  $\rightarrow$  IAU 2006/2000A. *Case* 

 $Case T = OP \rightarrow TEKS 08 C04. Case 2 EKP \rightarrow TEKS 08 C04 and X, T \rightarrow TAO 2000/2000A. Case 3 EOP \rightarrow USNO Finals$ 

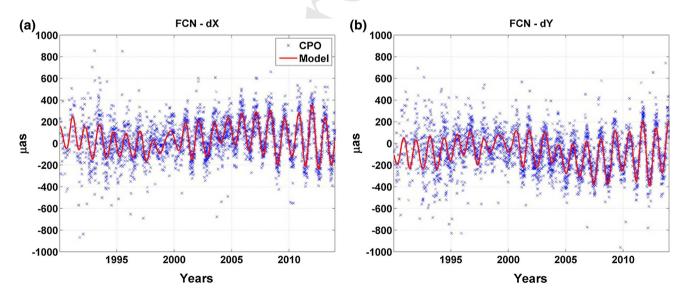


Fig. 4 *Blue dots* CPO estimated from IERS 08 C04 as a priori ERP and the Celestial Intermediate Pole (CIP) coordinates from the IAU 2006/2000A precession/nutation theory (*blue dots*). *Red line* Empirical Free Core Nutation (FCN) model plus the low-frequency part of the signal. *Units* µas

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WM and WRMS differences were estimated between case 1 410 and case 2 (with and without modification), once the FCN 411 was deleted (Fig. 3) (red line). It is noteworthy to mention 412 that the usage of the aforementioned model causes insub-413 stantial WM differences with a WRMS of about 80 µas in 414 the CPO; that reduction of the scatter by almost a half is 415 remarkable and the remaining variance seems to be attribut-416 able to the limitations of the theory and the models in terms 417 of unmodeled contributions. 418

#### 419 **3.3 Terrestrial reference frames**

The impact of using different TRFs to compute EOP solu-420 tions is assessed by fixing the station coordinates to their 421 a priori values taken from the respective catalogues. Fixing 422 the station positions entails somehow a deformation of the 423 actual network, since some unmodeled geophysical signals 424 still remain in every TRF apart from other possible sources 425 of uncertainty; however, this procedure is necessary here 426 to determine the differences between the investigated cat-427 alogues: if the coordinates would not be fixed on catalogue 428 values for this purpose, the VLBI data adjustment would 420 change the coordinates and we would not be able to assess the 430 consistency. Therefore, several EOP series were estimated 431 using the five terrestrial reference frames given in Table 5; 432 in all the cases, we took IERS 08 C04 as a priori EOP values 433 and fixed the radio source coordinates from ICRF2. Notice 434 that the estimates for each TRF (Fig. 5) are obtained using the same VLBI sessions, holding the  $3\sigma$  eligibility criterion for 436 all the implied frames, to achieve the maximum coherence 437 degree in the comparison. 438

The shift and drift of the EOP offsets provided by VieVS 439 using the different TRFs w.r.t. IERS 08 C04 were com-440 puted (Table 5) to compare the residuals associated with 441 each TRF with the ITRF2008 case. One of the most sig-442 nificant results for  $x_{pol}$  corresponds to the ITRF2000 case, 443 exhibiting considerable shift and drift  $(-123.9 \ \mu as and$ 444  $-16.8 \,\mu as \, year^{-1}$ , respectively), followed in magnitude by 445 its high drift in ITRF2005 ( $-9.0 \ \mu as \ year^{-1}$ ). Examining 446 the case of ITRF2005 is interesting, since it corresponds 447 to the most recent change of ITRF and EOP releases. It is 448 known that the seven-parameter rotation and rotation rates 449 relating ITRF2008 and ITR2005 vanish with the reported for-450 mal errors being of 8 µas. However, according to Sect. 3.5.1 451 of the IERS Annual Report 2011 (Dick 2013), the IERS 05 452 C04 series referred to ITRF2005 were re-aligned recogniz-453 ing the following biases, most of them given without formal 454 errors: "negligible" in  $x_{pol}$ ,  $-50 \pm 25 \ \mu as$  in  $y_{pol}$ , 2  $\ \mu s$  in 455 dUT1, and 1 and 17  $\mu$  as in dX, dY, respectively. Following 456 the same order and same units (for ITRF2005 in Table 5), we 457 find biases of values -25, 27, -1, -2, and 16, respectively, 458 but the remarkable novelty with respect to the presumed rel-459 ative orientation of the experiment results is the appearance 460

	$\Delta x_{\rm pol}~(\mu  {\rm as})$		$\Delta y_{\rm pol}~(\mu as)$		$\Delta dUT1 \ (\mu s)$		$\Delta X \ (\mu as)$		$\Delta Y(\mu as)$	
	Shift	Drift WI	WRMS Shift	Drift WRM	WRMS Shift I	Drift	WRMS Shift Drift		WRMS Shift Drift	WRMS
ITRF2008 <sub>fixed</sub>	$-17.5 \pm 8.2$	$-2.4 \pm 0.5$ 130	$-0.02 \pm 7.00$	TRF2008 <sub>fixed</sub> $-17.5 \pm 8.2$ $-2.4 \pm 0.5$ 130.9 $-0.02 \pm 7.2$ $1.2 \pm 0.5$ 120.3	$4.5\pm0.5$	$4.5 \pm 0.5  -0.2 \pm 0.03$	$8.1 - 2.2 \pm 4.4$	$8.1 - 2.2 \pm 4.4 \ 0.8 \pm 0.3 \ 77.2$	$15.9 \pm 4.5 - 3.3 \pm 0.3$	78.5
ITRF2005 <sub>fixed</sub>	$-25.2\pm8.7$	TRF2005 <sub>fixed</sub> $-25.2 \pm 8.7$ $-9.0 \pm 0.5$ 138.7	$3.7  27.1 \pm 7.9$	9 8.3 ± 0.5 131.3	$-0.9\pm0.5$	$0.2\pm0.03$	8.5 $-1.6 \pm 4.4$	8.5 $-1.6 \pm 4.4$ $1.0 \pm 0.3$ 77.9	$15.6 \pm 4.6 - 3.4 \pm 0.3$	78.9
ITRF2000 <sub>fixed</sub>	$-123.9 \pm 12.8$	TRF2000 <sub>fixed</sub> $-123.9 \pm 12.8 -16.8 \pm 0.8 236.1$	$5.1  118.3 \pm 10.4$	.4 $7.2 \pm 0.7$ 192.2	$1.2\pm0.6$	$-0.2\pm0.03$	$10.9 - 3.2 \pm 4.5$	$10.9 - 3.2 \pm 4.5  1.0 \pm 0.3  79.0$	$14.7 \pm 4.6 - 3.4 \pm 0.3$	80.5
VTRF2008 <sub>fixed</sub>		$29.6 \pm 7.8 \qquad -1.4 \pm 0.5  124.4$		$28.1 \pm 7.2  21.9 \pm 0.5  119.8$	$-0.6 \pm 0.5 -0.03 \pm 0.03$	$-0.03\pm0.03$	$8.2 - 1.6 \pm 4.3$	8.2 $-1.6 \pm 4.3$ 0.7 $\pm$ 0.3 76.3	$15.6 \pm 4.6 - 3.3 \pm 0.3$	77.9
DTRF2008 <sub>fixed</sub>	$-51.4 \pm 7.9$	DTRF2008 <sub>fixed</sub> $-51.4 \pm 7.9$ $0.5 \pm 0.5$ $123.7$	$1.7  11.3 \pm 7.1$	$11.3 \pm 7.1$ $0.1 \pm 0.5$ $118.2$	$-5.5 \pm 0.5 - 0.08 \pm 0.03$	$-0.08\pm0.03$	$8.1 - 1.7 \pm 4.4$	$8.1  -1.7 \pm 4.4  0.8 \pm 0.3  76.9$	$16.1 \pm 4.5 - 3.3 \pm 0.3$	78.3

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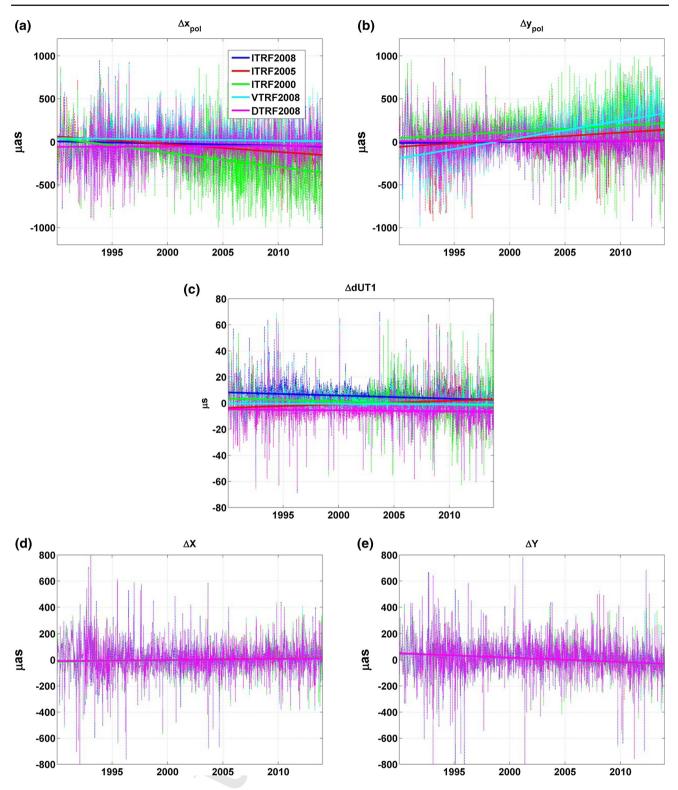


Fig. 5 EOP differences w.r.t. IERS 08 C04 between solutions using different terrestrial reference frames (*blue* ITRF2008, *red* ITRF2005, *cyan* VTRF2008, *magenta* DTRF2008 and *green* ITRF2000). *Straight lines* represent the corresponding linear trends. *Units* µas or µs for dUT1

<sup>461</sup> of non-negligible drifts, two of them reaching the 8–9  $\mu$  as <sup>462</sup> year<sup>-1</sup>magnitude. That issue is addressed in Sect. 3.5 from <sup>463</sup> a different perspective to get more insight. Relevant weakness for the  $y_{pol}$  parameter appears in 464 VTRF2008 and ITRF2000, with a trend bigger than 20  $\mu$ as 465 year<sup>-1</sup> and an important shift of 118.3  $\mu$ as, respectively. Con-

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<sup>467</sup> cerning DTRF2008 and the ERP, the maximal shift occurs in <sup>468</sup> dUT1, exceeding  $-5.5 \,\mu$ s; the shift of  $x_{pol}$  reaches  $-51 \,\mu$ as. <sup>469</sup> Finally, trends and biases of the CPOs are close in all the <sup>470</sup> cases and smaller than those of the ERPs. The maximum scat-<sup>471</sup> ter and minimum scatter (WRMS after subtracting the linear <sup>472</sup> component of the difference w.r.t. IERS 08 C04 series) of the <sup>473</sup> EOP correspond to ITRF2000 and DTRF2008, respectively.

ITRF2000 presents large WM and WRMS in  $x_{pol}$ ,  $y_{pol}$ , 474 and dUT1. Further interesting results are found for the 475 VTRF2008 case, with large WM (-133.8 µas), WRMS 476 (113.0  $\mu$ as), for y<sub>pol</sub>; that seems to be due to the contrast 477 between multi-technique (ITRF2008) vs single-technique 478 (VTRF2008) approaches. DTRF2008 shows large WM (10.5 479 μs) for dUT1, which is remarkable, because both ITRF2008 480 and DTRF2008 are based on the same input data and accord-481 ingly, they only differ in the weighting of the techniques and 482 the local ties among each other and in the datum definition. 483 Celestial pole coordinates in all the cases do not show notice-484 able systematic effects, with small WM and WRMS (5 and 485 10 µas, respectively). It is evident that the CPO are insensi-486 tive to TRF changes unlike the ERP, within the accuracy and 487 stability limits set by GGOS. 488

#### **3.4 Celestial reference frames**

Other EOP solution series were calculated using two dif-490 ferent Celestial Reference Frames (ICRF2 and ICRF-Ext.2, 491 Table 1) to study the sensitivity of VLBI EOP to the a pri-492 ori CRF. In this part, the conventional terrestrial reference 493 frame (ITRF2008 fixed on its a priori values) was used for 494 the VLBI analysis, together with the IERS 08 C04 as a pri-495 ori EOP. As in the previous sections, the difference between 496 both approaches is assessed by means of WM and WRMS. 497 According to our estimates, the impact of using two differ-498 ent ICRFs on EOP is about at the level of stability of the 499 ICRF2 axes relative to ICRF-Ext.2 (10 µas) with WRMS 500 EOP differences of about 40 µas (Table 6). The fact that 501 errors in source positions affect EOP in a much lesser extent 502 than errors in station position is not unexpected at all, since in 503 ordinary VLBI sessions, the number of observed sources is 504 much larger than the number of participating stations. It also 505 empirically confirms that the statistics given for the ICRF2 506 are correct and it proves that the additional including of about 507 15 years of VLBI observations (comparing ICRF-Ext.2 and 508 ICRF2) does not lead to systematic rotations of the ICRF. 509 Shifts and drifts of the differences between both ICRF solu-510 tions (reported in Table 6) present analogous results for both 511 studies, where the largest WRMS of the linear regression can 512 be found on the EOP corresponding to ICRF-Ext.2 and the 513 maximal EOP differences appear for the CPO with a shift of 514 10.3  $\mu$ as in X and drift of 0.9  $\mu$ as year<sup>-1</sup> in Y, close to the 515 values reported in Table 3 of Heinkelmann et al. (2015) for 516 the period 1984 to 2013. 517

**Table 6**EOP Differences ( $\mu$ as or  $\mu$ s for dUT1) between EOP estimatedwith ICRF2 and ICRF1 ext. 2

EOP	Case 2 vs. case 1		
	Shift	Drift	WRMS
$\Delta x_{\rm pol} (\mu as)$	$5.0 \pm 3.1$	$0.5 \pm 0.2$	51.1
$\Delta y_{\rm pol}$ (µas)	$-7.9\pm2.5$	$0.5\pm0.2$	41.3
$\Delta dUT1 \ (\mu s)$	$1.0 \pm 0.1$	$0.0 \pm 0.01$	1.6
$\Delta X (\mu as)$	$-10.3\pm2.6$	$-0.7\pm0.1$	45.5
$\Delta Y(\mu as)$	$4.1\pm3.2$	$-0.9\pm0.2$	56.4

Shift (referred at epoch J2000.0) and linear trends (year<sup>-1</sup>) are estimated by WLS. The WRMS are computed after subtracting the linear component of the difference

### 3.5 Similarity transformation vs. VLBI ERP differences 518

Going back to the tests performed in Sect. 3.3 and recall-519 ing the comments relative to the ITRF2005 case, it seems 520 clear that those results show that the differences among EOPs 521 derived using distinct ITRFs cannot be explained simply by 522 the nominal Helmert transformation between the implied 523 frames. This could be surprising at first glance, but our analy-524 sis is performed with the series of VLBI individual sessions. 525 Each session involves a small number of stations compared 526 with the number of defining ITRF stations and their geo-527 graphical distribution is not homogeneous at all. It makes 528 sense to consider separately the sub-networks of stations 529 participating at each session to define a suitable epoch-530 frame associated specifically to each session. To investigate 531 whether the EOP differences determined in the previous 532 Sect. 3.3 can be attributed to the differences in orientation 533 of those particular frames to some extent, the correspond-534 ing six Helmert transformation parameters were estimated 535 per each VLBI session using WLS. We computed the trans-536 formation parameters of the various frames given in Table 537 2 w.r.t. ITRF2008 for each individual station subset of the 538 included VLBI session: three translation components, and 539 three rotation angles, designated,  $T_x$ ,  $T_y$ ,  $T_z$ ,  $R_1$ ,  $R_2$ , and  $R_3$ , 540 respectively. The scale factor is not determined to be consis-541 tent with the VLBI estimates, which have been calculated 542 fixing the station coordinates. Equation (3) shows the sim-543 ilarity transformation applied, where  $x_i$ ,  $y_i$ , and  $z_i$  are the 544 Cartesian coordinates of the *i*-th point common in the two 545 reference frames, ITRF2008 and each considered alternative 546 TRF: 547

$$\begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{\text{ITRF2008}} = \begin{pmatrix} T_x \\ T_y \\ T_z \end{pmatrix} + R \begin{pmatrix} x_i \\ y_i \\ z_i \end{pmatrix}_{\text{TRF}}.$$
 (3) 548

Let us insist that this transformation is between subnetworks, not between the relevant TRFs, although we use an 550

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abridged notation that makes no reference to sessions. The 551 transformation parameters per each VLBI session were esti-552 mated after each subset of station coordinates was brought 553 at the same VLBI epoch using its own station motion model 554 (considering the a priori catalogue positions and velocities) 555 as performed in Feissel et al. (1993). To make sure that each transformation was consistent with the VLBI estimates, each 557 Helmert estimate was computed with the same stations that 558 appear in each VLBI session included in the analyses of 559 Sect. 3.3. For the comparison, the derived ERP (Sect. 3.3) 560 were expressed as global rotations using 561

562 
$$R_1 = -y_{\text{pol}}$$
  $R_2 = x_{\text{pol}}$   $R_3 = r' \cdot \text{dUT1} - \text{A}_3$ 

where we assumed the rotational contribution from the ICRF to dUT1 to be negligible ( $A_3 = 0$ ) due to the relative insensitivity of dX and dY to TRF changes described in Sect. 3.3. Here,  $r' \approx 0.997$  denotes the ratio between solar and sidereal time.

Table 7 summarizes the statistics of the differences 568 between estimated similarity transformation parameters and 569 estimated VLBI ERP differences for each TRF of Table 5; 570 they are expressed as global rotations in both the cases and 571 referred to ITRF2008 in terms of their relative linear regres-572 sions and standard deviations (STD) of their differences. 573 Differences are always computed, so that the ERP series esti-574 mated from ITRF2008 are the minuend. 575

The most relevant results are: (1) ITRF2000 presents con-576 siderable drift for  $R_2$  (-17.4 µas year<sup>-1</sup>) and shifts in all 577 the rotations; (2) between ITRF2005 and ITRF2008, there are 578 still significant shifts. This is astonishing, because ITRF2008 579 orientation and orientation stability are defined by no-net 580 rotation (NNR) with respect to ITRF2005. Obviously, the 581 NNR condition (kinematically non-rotation) that is based on 582 a subset of stations common for ITRF2005 and ITRF2008 583 does not exactly force non-rotation for another subset of sta-584 tions, such as the VLBI station subset, used in our study; 585 (3) another interesting results are found for the VTRF2008 586 case, with large drift (19.9  $\mu$  as year<sup>-1</sup>) for  $R_1$ ; (4) DTRF2008 58 shows a large shift (173.0 µas) for dUT1; (5) drifts and shifts 588 are very similar in both approaches; and (6) for DTRF2008 589 and VTRF2008, the STD are about 20 µas probably caused 590 by an incomplete atmosphere modeling and inaccuracies of 591 the station coordinates; and for ITFR2005 and ITFR2000, 592 the STD are larger, reaching around 50 µas in the last case. 593 The smallest STD can be found comparing ITRF2008 to 594 DTRF2008. Let us recall that the results labelled as Helmert 505 trans. in Table 7 do not involve VLBI data, whereas the block 596 labelled as VLBI is computed from EOP VLBI solutions. The 597 similarity of shifts and drifts (pointed in 5) and the magnitude of the STD (described in 6) prove that the VLBI data 599 analysis can work as an accurate tool to determine frame 600 inconsistencies. 601

#### 4 Summary and conclusions

An experimental study has been carried out addressing the consistency of the current conventional reference frames (ITRF2008 and ICRF2) and the associated IERS 08 C04 series. Since we are concerned with all five EOP, the only technique that can be applied is VLBI.

Concerning the study on the effects of the unmodeled geo-608 physical signals conducted in Sect. 3.1, one can say that these 609 neglected signals induce damaging effects on the terrestrial 610 pole coordinates and dUT1, causing a strong decrease of the 611 correlation among EOP based on fixed coordinates and EOP 612 based on adjusted coordinates with a priori from ITRF2008. 613 Maximal differences affect  $y_{pol}$  and are a 26.9 µas shift and 614 a 2.1  $\mu$ as year<sup>-1</sup> drift (Table 3). These values give an idea of 615 how good the ITRF2008 is. 616

The EOP estimated by VLBI analysis might, in addi-617 tion, depend on the choice of the a priori EOP, and thus, we 618 investigated that possibility. Here, we compare EOP adjust-619 ment with respect to IERS 08 C04 when using IERS 08 620 C04, USNO finals, or the astronomical conventional pre-621 cession/nutation models, IAU2006/2000A. The comparison 622 between EOP estimated using IERS 08 C04 and USNO 623 finals exhibits a large scatter of dUT1 at the level of 5.3 µs 624 (Table 4). 625

VTRF2008 is consistent with ICRF-Ext.2 which contains 626 precise positions of more than 3000 compact radio astronom-627 ical sources. Different EOP series are estimated with identical 628 VLBI solutions, but with different celestial reference frames 629 (ICRF2 and ICRF-Ext. 2) to analyze their mutual stability. 630 The maximal EOP differences (10.3  $\mu$ as at  $\Delta X$  and 0.9  $\mu$ as 631 year<sup>-1</sup> at  $\Delta Y$ ) (Table 6) fulfill the stability goal for celes-632 tial pole offsets of about 10 µas. Therefore, the ICRF2 and 633 ICRF-Ext.2 orientations can be assumed identical within this 634 uncertainty, which is below the threshold of accuracy targeted 635 by GGOS and associated working groups. 636

However, when the EOP are estimated by fixing sta-637 tion positions on various terrestrial reference frames, serious 638 inconsistencies are detected with respect to ITRF2008 (Table 639 7). ITRF2000 and ITRF2005 are included in this compari-640 son, because the orientation of ITRF2008 is realized by NNR 641 conditions with respect to the orientation of the ITRF2005, 642 which in its turn is realized via NNR condition with respect 643 to ITRF2000. Although the ITRF2008 and the ITRF2005 644 are constrained to be kinematically non-rotating with an 645 uncertainty of 8  $\mu$ as and 8  $\mu$ as year<sup>-1</sup>, meaningful differ-646 ences above this level and even larger discrepancies with 647 respect to ITRF2000 are found (in particular in the terrestrial 648 pole coordinates) based on the VLBI subset of stations. A 649 marked inconsistency is the differential drift in  $y_{pol}$  of about 650  $-19.9 \ \mu$ as year<sup>-1</sup>, between VTRF2008 and ITRF2008; it 651 means that ICRF2, ITRF2008, and the conventional EOP 652 series are not completely consistent. ITRF2000 shows large 653

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Table 7Global rotations $(R_1, R_2, \text{ and } R_3)$  for each VLBIsession from similaritytransformation and ERPdifferences between ITRFs w.r.t.ITRF2008 based VLBIsolutions

	Helmert trans.	(µas)	VLBI (µas)		Comparison (µas)
	Shift	Drift	Shift	Drift	STD
ITRF2005					
<i>R</i> 1	$20.9\pm9.4$	$8.8\pm0.6$	$30.9\pm8.9$	$8.9\pm0.6$	26.0
R2	$21.3\pm6.6$	$-7.9\pm0.4$	$12.2\pm6.3$	$-7.8\pm0.4$	29.3
<i>R</i> 3	$121.4\pm4.7$	$-8.9\pm0.3$	$108.4\pm4.3$	$-8.1\pm0.3$	25.0
DTRF2008					
<i>R</i> 1	$-1.0\pm1.3$	$0.2\pm0.1$	$8.7\pm1.3$	$-0.4\pm0.1$	20.7
<i>R</i> 2	$-36.2\pm0.8$	$1.9\pm0.1$	$-31.3 \pm 1.1$	$1.9\pm0.1$	18.1
R3	$172.7\pm0.7$	$-3.1\pm0.1$	$173.0\pm0.9$	$-3.0\pm0.1$	13.5
VTRF2008					
<i>R</i> 1	$19.8\pm1.7$	$19.8\pm0.1$	$27.9 \pm 1.5$	$19.9\pm0.1$	21.8
<i>R</i> 2	$47.1\pm1.5$	$1.6\pm0.1$	$48.9 \pm 1.4$	$1.2\pm0.1$	21.4
<i>R</i> 3	$96.3\pm0.9$	$-0.5\pm0.1$	$92.9\pm0.9$	$-1.3\pm0.1$	16.7
ITRF2000					
<i>R</i> 1	$112.9\pm9.0$	$5.7\pm0.7$	$123.5\pm8.3$	$6.1\pm0.6$	50.3
<i>R</i> 2	$-77.2\pm8.2$	$-17.8\pm0.6$	$-89.6\pm8.9$	$-17.4\pm0.7$	51.4
<i>R</i> 3	$80.0\pm4.2$	$-1.1 \pm 0.3$	$80.0\pm4.8$	$-1.9\pm0.4$	41.0

Shifts (referred to epoch J2000.0) and linear drifts (year<sup>-1</sup>) are estimated by LS

The comparison between these two approaches is made by the standard deviation (STD) of the EOP differences

shifts in  $x_{pol}$  and  $y_{pol}$ , and a considerable drift of about 17.4 654  $\mu$ as year<sup>-1</sup> in x<sub>pol</sub>. Besides, dUT1 evidences substantial 655 inconsistency problems in all tested TRFs, the most pro-656 nounced results being between ITRF2008 and DTRF2008 657 (more than 5 mm at the Earth equator). These detrimental 658 effects could come from unconsidered geophysical signals 659 (e.g., non-tidal ocean loading), which are neglected and need 660 to be identified. In contrast, celestial pole coordinates, in all 661 the cases, do not show noticeable systematic effects. 662

Summarizing, in the last 30 years, the EOP accuracy
has reached levels, where the margin of improvement is
extremely limited. In spite of this enhancement, our study
confirms the conclusion that neither the IERS EOP series
nor the ITRFs considered in our tests are accurate enough to
meet the GGOS goals.

In spite of the valuable advances along many years, the 669 consistency resulting from the combination process contin-670 ues being at least debatable, considering the extreme dif-671 ferences of the weights assigned to the solutions depending 672 on the various techniques and EOP. Namely, the Interna-673 tional GNSS Service (IGS) solution contributes to the ERP 674 by about 95 %, but nothing to the offsets of the Celestial 675 Intermediate Pole, which is based only on VLBI results. The 676 latter are ignored in the combination and added later for the 677 sake of completeness. Moreover, the orientation of the VLBI 678 ground network that refers to the ICRF via the VLBI EOP 679 is allowed to rotate during the combination. Consequently, 680 we can infer that the IERS 08 C04 do not refer exactly to 681

ICRF. Other potential causes of inconsistency are the current 682 methodology of inheriting the orientation from the previous 683 realization to the current realization by applying the NNR 684 condition, i.e., the new frame inherits the "errors" of all its 685 predecessors and adds its own errors. Inconsistencies are also 686 due to the misfit of the true station coordinates and the sim-687 ple coordinate model used for its approximation, i.e., the 688 uncorrected non-linear station displacement will propagate 689 into EOP, since non-linear effects are not removed. These 690 causes could be among the reasons why the optimum con-691 sistency level is not being accomplished yet. Proposals to 692 achieve higher accuracy and consistency are that the ITRF, 693 the EOP, and the ICRF have to be determined in one mono-694 lithic adjustment, including all observations of all involved 695 techniques (VLBI, DORIS, GNSS, and SLR), the usage of 696 epoch reference frames (Bloßfeld et al. 2014), and extend-697 ing the TRF coordinate model to include seasonal signals, 698 as it is foreseen for the next realization of ITRS, ITRF2014 699 (Altamimi et al. 2016). 700

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