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PITFALLS ON COMPUTING LIQUID-LIQUID PHASE EQUILIBRIA USING THE K-VALUE METHOD
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## Summary

In the past, many strategies have been proposed to solve liquid-liquid equilibrium (LLE). Nevertheless, some papers and process simulation software packages still show inconsistent procedures for LLE regressions that lead to apparent solutions which are not true tie-lines. This study illustrates some of the pitfalls of the LLE data correlation and proposes some ideas to overcome them.

## Isoactivity criterion

$\checkmark$ The necessary but not sufficient isoactivity criterion (K-value method) is the most frequently used equilibrium condition for LLE calculations.

## Minor common tangent criterion

$\checkmark$ It specially fails when the Gibbs energy of mixing function $\left(\mathrm{g}^{\mathrm{M}}\right)$ is very linear between the equilibrium
The Gibbs minor common tangent criterion is the necessary and sufficient condition for points or when the equilibrium compositions are very close

## Convergence efficiency comparison in LLE calculations

The following example illustrates the problem: methanol (1) + diphenylamine (2) + cyclohexane (3) system at $25^{\circ} \mathrm{C}$. More precisely, the tie-line obtained from the global mixture $\mathrm{M}\left(\mathrm{z}_{1}=0.5365 ; \mathrm{z}_{2}=0.0230 ; \mathrm{z}_{3}=0.4405\right.$, molar fractions) will be calculated. The NRTL model is used with $\alpha=0.2$ and the values for the binary interaction parameters obtained from DECHEMA Chemistry Data Series [1].
$\checkmark$ The activity objective function (O.F.(a)) is evaluated close to the LLE solution (Figure 1). A variety of false tie-lines can be obtained that correspond with very low values of the activity objective function although, obviously, the true tie-line is unique.
The activity function provides a poor definition of the objective function minimum (O.F.(a) $<10^{-12}$ in Figure 2), because the $\mathrm{g}^{\mathrm{M}}$ surface for this system is very flat.

$$
\begin{equation*}
\text { O.F. }(a)=\sum_{i=1}^{3}\left(a_{i}^{1}-a_{i}^{I I}\right)^{2}=0 \tag{1}
\end{equation*}
$$

$\checkmark$ Next, a combination of the activity and the minor common tangent condition (O.F.(t) in Figure 2) based on Iglesias-Silva et al. [2] is used, and a sharper minimum for the objective function value is obtained. The common tangent line contribution to the objective function is:

$$
\begin{equation*}
\text { O.F. }(\mathrm{t})=\left[\left(\frac{\partial \mathrm{g}^{\mathrm{M}}}{\partial \mathrm{x}_{3}}\right)_{\mathrm{p}, \mathrm{~T}, \mathrm{D}}^{\mathrm{I}}-\left(\frac{\partial \mathrm{g}^{\mathrm{M}}}{\partial \mathrm{x}_{3}}\right)_{\mathrm{p}, \mathrm{~T}, \mathrm{D}}^{\mathrm{II}}\right]^{2}+\left[\left(\mathrm{g}^{\mathrm{MI}}-\mathrm{g}^{\mathrm{MII}}\right)_{+}+\left(\left(\frac{\partial \mathrm{g}^{\mathrm{M}}}{\partial \mathrm{x}_{3}}\right)_{\mathrm{p}, \mathrm{~T}, \mathrm{D}}^{\mathrm{I}} \quad-\left(\frac{\partial \mathrm{g}^{\mathrm{M}}}{\partial \mathrm{x}_{3}}\right)_{\mathrm{p}, \mathrm{~T}, \mathrm{D}}^{\mathrm{D}}\right)_{\mathrm{x}_{3}}\right] \quad \mathrm{D}=\frac{\mathrm{x}_{2}^{\mathrm{II}}-\mathrm{x}_{2}^{\mathrm{I}}}{\mathrm{x}_{3}^{\mathrm{II}}-\mathrm{x}_{3}^{\mathrm{I}}}=\frac{\mathrm{x}_{2}^{\mathrm{M}}-\mathrm{x}_{2}^{\mathrm{I}}}{\mathrm{x}_{3}^{\mathrm{M}}-\mathrm{x}_{3}^{\mathrm{I}}} \tag{2}
\end{equation*}
$$

## PROPOSED METHOD

$\checkmark$ Finally, we present a modification of the vector method [3] developed by Eubank et al. [4]. The original work used the vector method combined with the maximum area criterion as equilibrium condition (later proved to be only applicable for binary systems [5]).

Our algorithm, that is applicable to the ternary systems, uses the minor common tangent equilibrium condition (O.F.(t)) [2]:

- An $\alpha$-angle range for each ternary global mixture M (Figure 3) is defined.
- For a sheaf of straight lines passing through M, the two common tangent points (I, II) to the $\mathrm{g}^{\mathrm{M}}$ function in the corresponding sectional plane are obtained (necessary condition)
- Among all pairs of calculated compositions, the "true" tie-line corresponds to the O.F.(a) equal to zero (sufficient condition) which corresponds to the minimum value for the Gibbs energy of mixing ( $\mathrm{g}^{\mathrm{TL}}$ ).


Figure 3. Graphical representation of the suggested method
$\checkmark$ The O.F.(a) is evaluated for each $\alpha$-angle at the two common tangent points. Those values (suggested method O.F.(a)) are compared to the other previous approaches (Figure 2) showing that a sharper minimum is obtained.

## References:

$\checkmark$ [1] Sørensen, J.M.; Artl, W. DECHEMA Chemistry Data Series, Vol. V: Frankfurt, 1980.
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$\checkmark$ [4] Eubank, P.T.; Elhassan, A.E.; Barrufet, M.A.; Whiting, W.B. Ind. Eng. Chem. Res. 1992, 31, 942.
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## RESULTS

$\checkmark$ When the activity condition is combined with the common tangent line criterion, either simultaneously (eq 2) or sequentially (vector method), a more efficient equilibrium calculation can be carried out, avoiding false solutions with very low values of the O.F.(a)).
$\checkmark$ The suggested method improves the convergence of the optimization.

