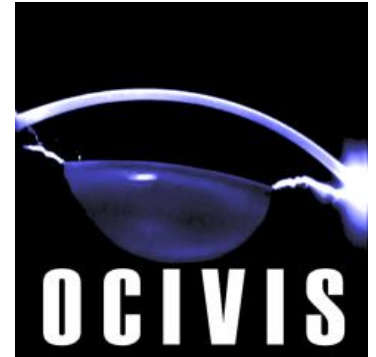


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***Look-up table of quadrics
applied to
corneal topography***

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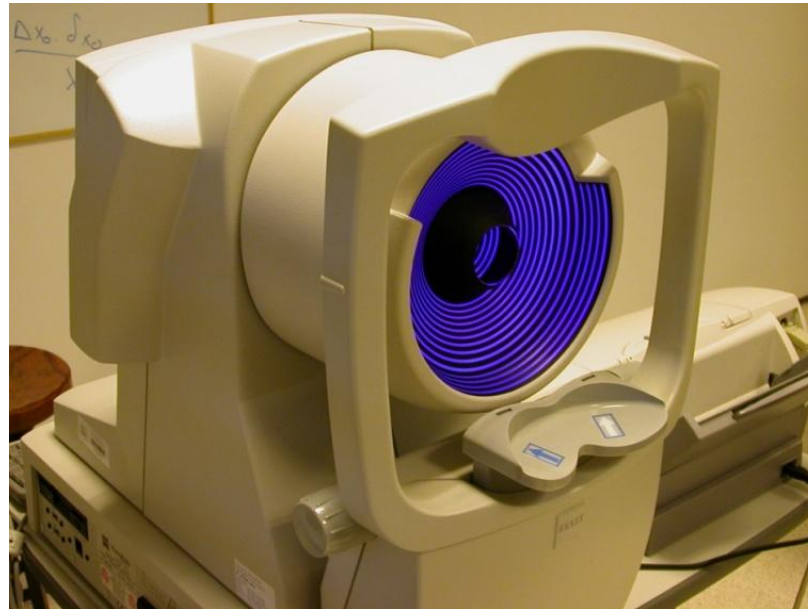
INTRODUCTION

CLASSIC INSTRUMENTS:

- Topography maps → Placido rings

MODERN INSTRUMENTS:

- Normal/Pathological shapes
- Contact lens fitting
- Refractive surgery



ADVANTAGE

- Videokeratometers → useful information about corneal topography and tear film

DISADVANTAGES

- Not control of camera and processing algorithms
- HIDDEN information
- Cartesian to polar coordinates → extrapolating corneal data

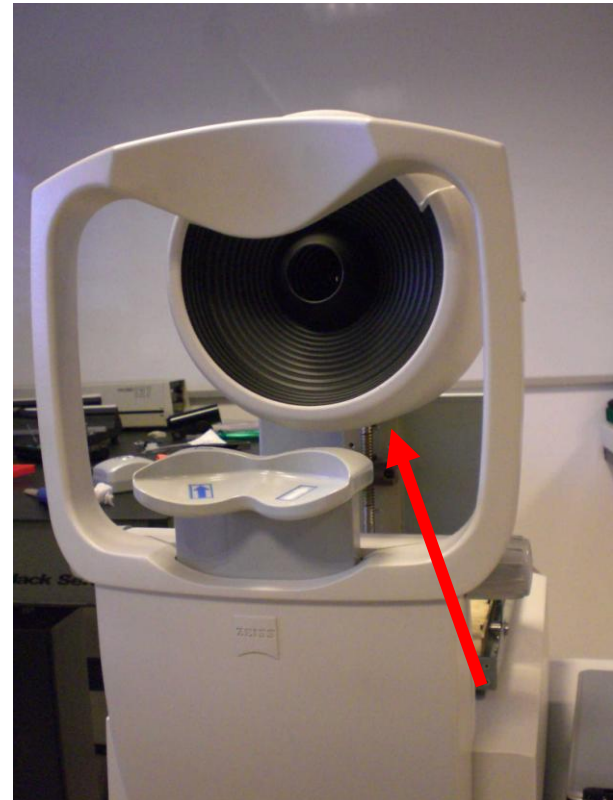
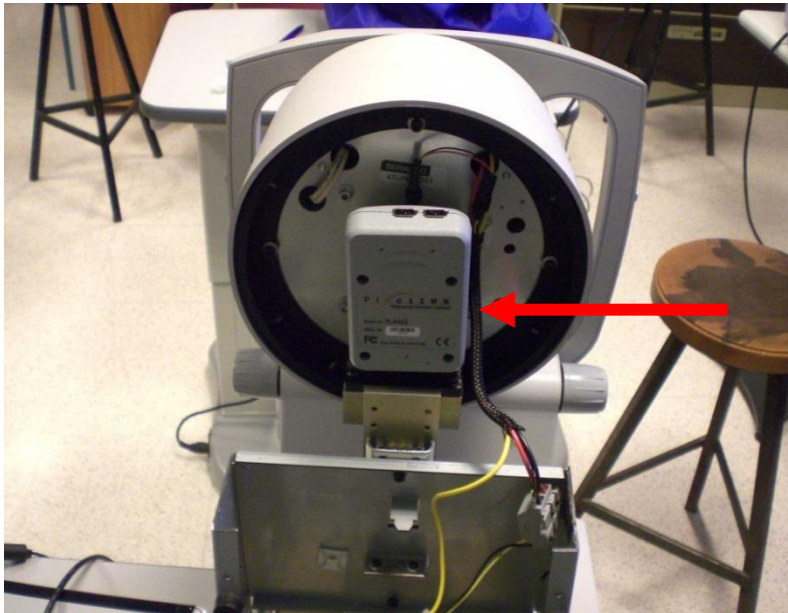
- New look-up table method to convert acquired corneal data from reflected Placido rings to curvature radii
 - * Full control algorithm and information
 - * No extrapolation

WHAT WE DO?

- TO CALIBRATE A TOPOGRAPHER HEAD
- PROCESSING ALGORITHM
 - * RINGS EXTRACTION
 - * RINGS LABELLING
 - ELLIPTICAL SCANNING ALGORITHM

EXPERIMENTAL SETUP

- Corneal topographer → Humphrey Atlas 995 of Zeiss Meditec, 22 rings and IR light
- Video Camera → CMOS color camera PL-A662 FireWire PixeLINK with 1Mpx
- CCD → back of the head



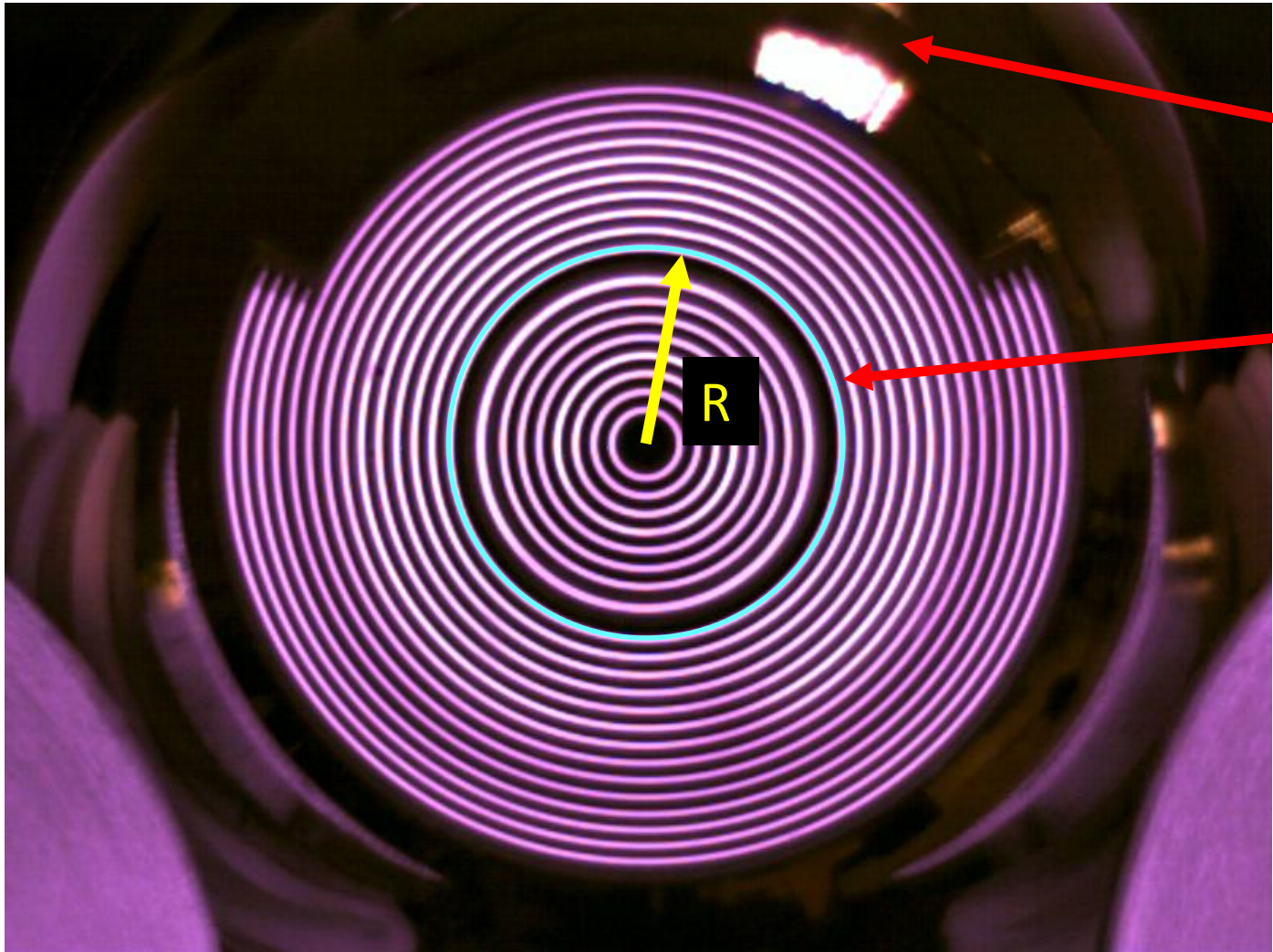
CALIBRATION PROCESS

- Corneal reflection of Placido ring → keratometric principle as

$$R = \frac{hC}{2z}$$

- 16 steel spheres
- Spheres in front of topographer → reflected Placido rings on each one





Sphere C=8 mm

Ring nº 9
R(px)

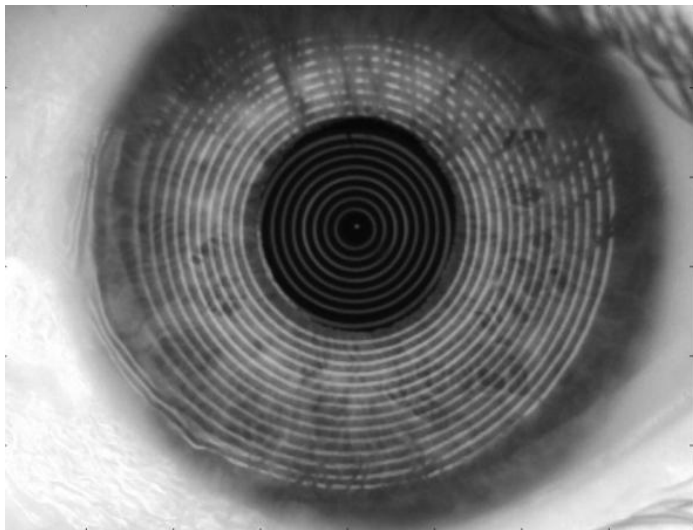
$$R = \frac{hC}{2z}$$

RING EXTRACTION

- **Placido rings** → eyes surface
- **Open top-hat** : detect wave crest $OTH_{FB} = (F - F \circ B)$
- **Close top-hat** : detect wave hollow $CTH_{FB} = (F \cdot B - F)$

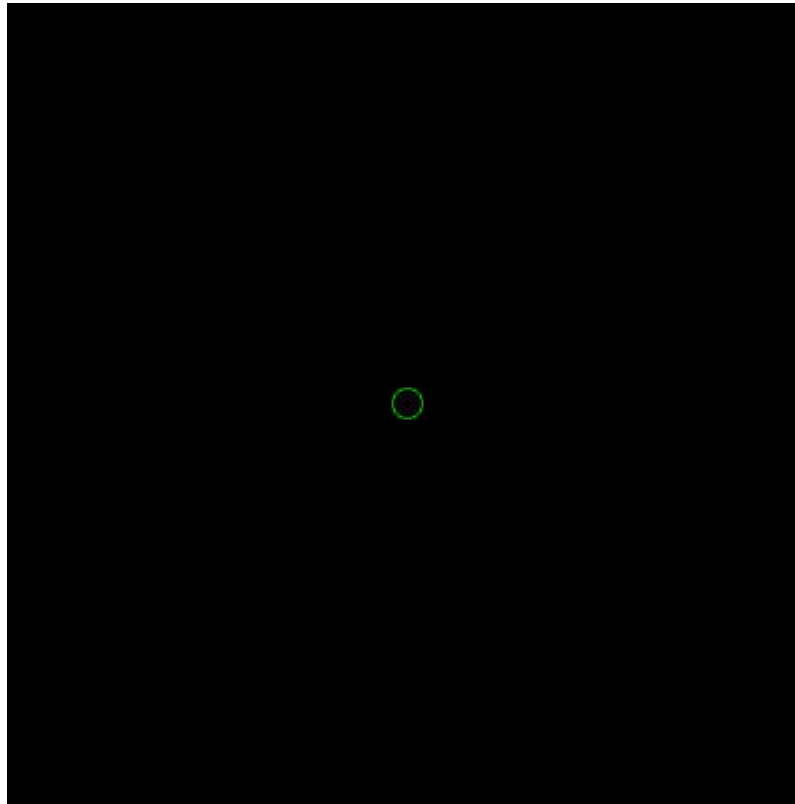
To Improve Contrast

(Open Top-Hat) – (Close Top-Hat)



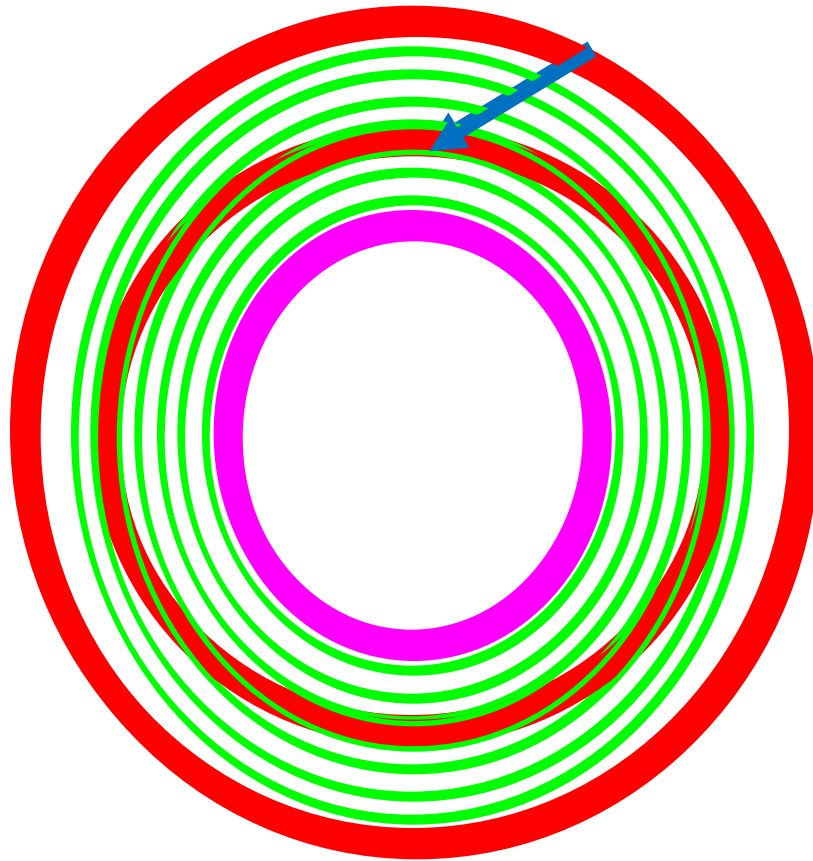
RINGS LABELLING

Elliptical scanning algorithm



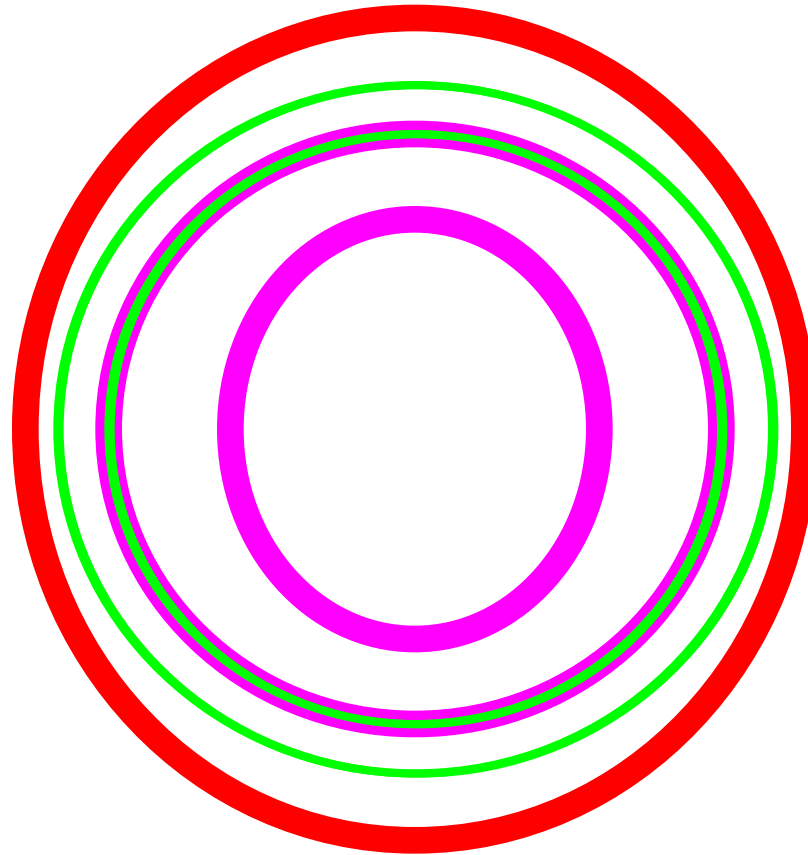
RINGS LABELLING

Elliptical scanning algorithm



RINGS LABELLING

Elliptical scanning algorithm



CALIBRATION EQUATIONS

- Curvature surface

$$R = \frac{hC}{2z}$$

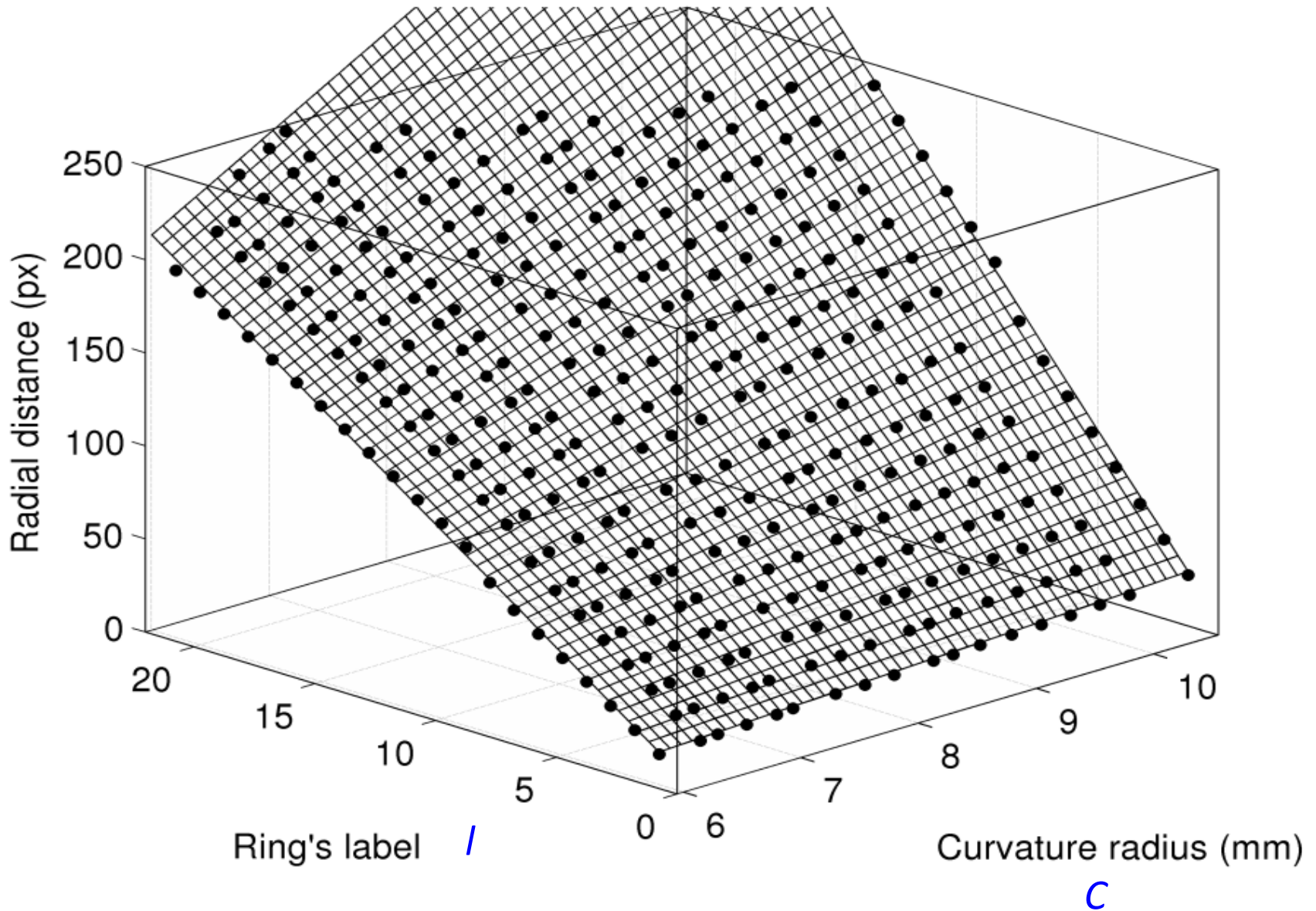
$$\frac{h}{2z} = al + b$$

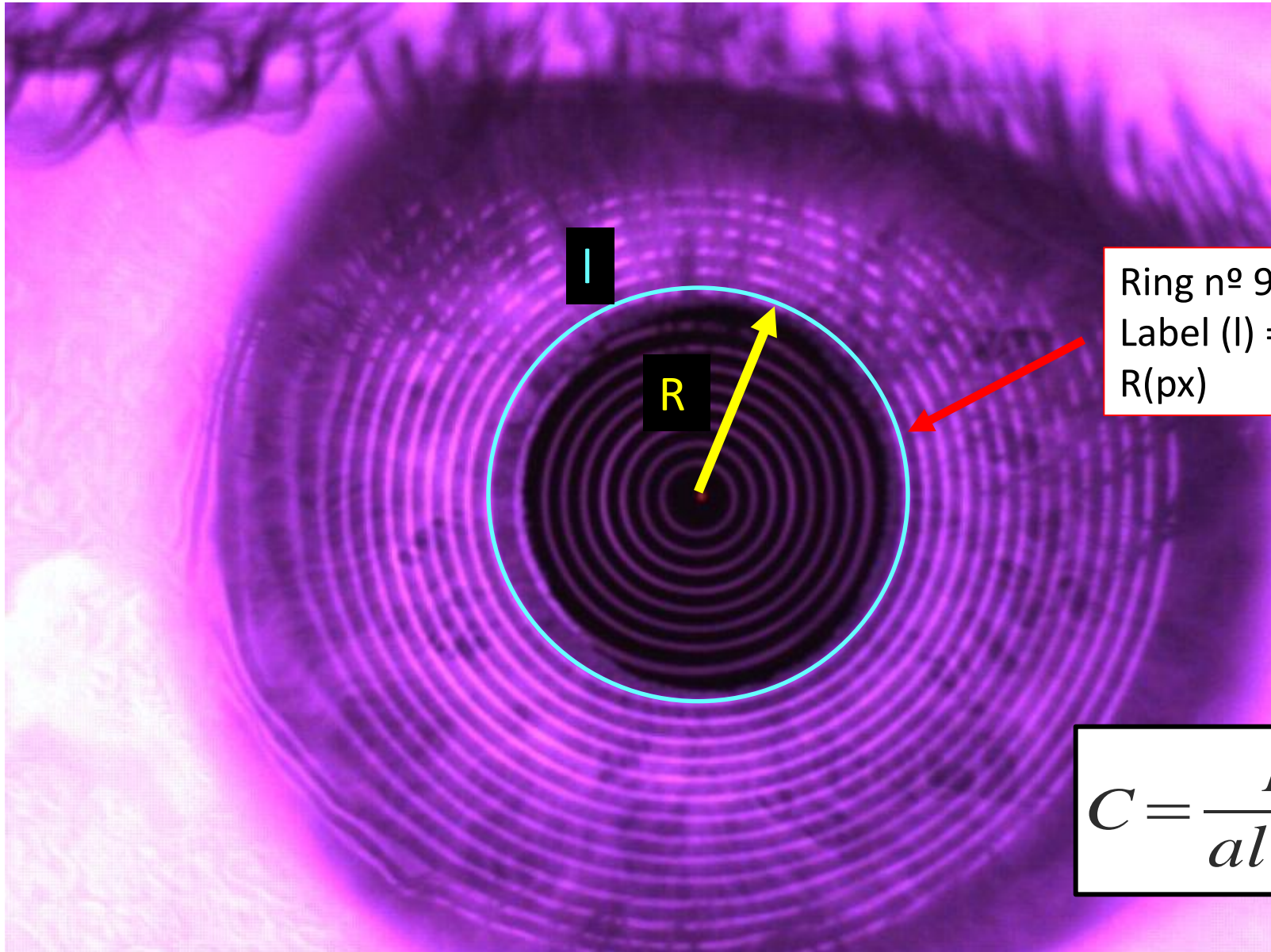
$$R = (al + b)C$$

- 3 variables

- * Independent variable l (ring's label) and curvature radius C
- * Radial distance R from fitting to a circle
- * Coefficients (a) and (b) → least square fitting

CALIBRATION EQUATIONS





Ring nº 9
Label (l) =9
R(px)

$$C = \frac{R}{al + b};$$

CALIBRATION EQUATIONS

- Curvature radius $C(x,y)$, no $C(R)$

$$C = \frac{R}{al+b};$$

$$C(x, y) = \frac{R(x, y)}{(al+b)}$$

$$(x, y) \in Ring_l$$

$$R = \frac{hC}{2z};$$

$$R^2 = x^2 + y^2; \quad R = m_l C + n_l$$

- Quadric equation:

$$x_l^2 + y_l^2 = m_l^2 C^2 + 2m_l n_l C + n_l^2$$

$$v_l D_l v_l^T + E_l v_l^T + F_l = 0$$

$$V_l = \{x_l, y_l, c\}$$

- Calibration equation for each ring

$$C(x, y) = (d_l x + e_l y + h_l + G_l(x, y)) / 2$$

with:

$$G_l(x, y) = ((d_l x + e_l y + h_l)^2 + 4(a_l x^2 + c_l xy + f_l x + b_l y^2 + g_l y + k_l))^{(1/2)}$$

- C and (x_l, y_l) coordinates of data for each l ring
→ least-squares fitting.

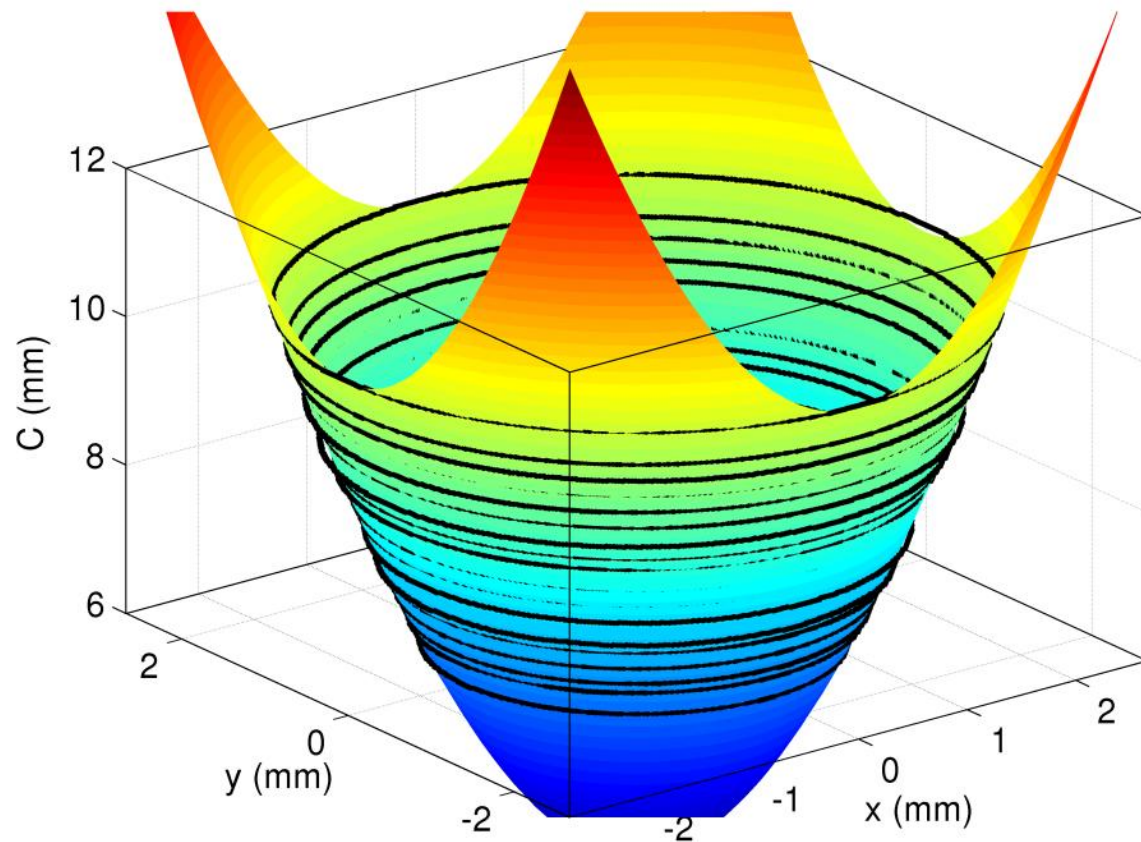
LOOK-UP TABLE OF QUADRICS

- Results for the fitting of ring 16

a_{16}	40.78(38.99,42.57)	f_{16}	3.01(2.67,3.34)
b_{16}	40.88(39.09,42.68)	g_{16}	1.10(0.07,1.41)
c_{16}	-0.08(-0.13,-0.04)	h_{16}	-26.16(-28.04,-24.29)
d_{16}	-0.35(-0.39,-0.31)	k_{16}	92.43(85.47,99.38)
e_{16}	-0.11(-0.14,-0.07)		

Parameters and confidence bounds of 95%

Data and surface resulting from the fitting

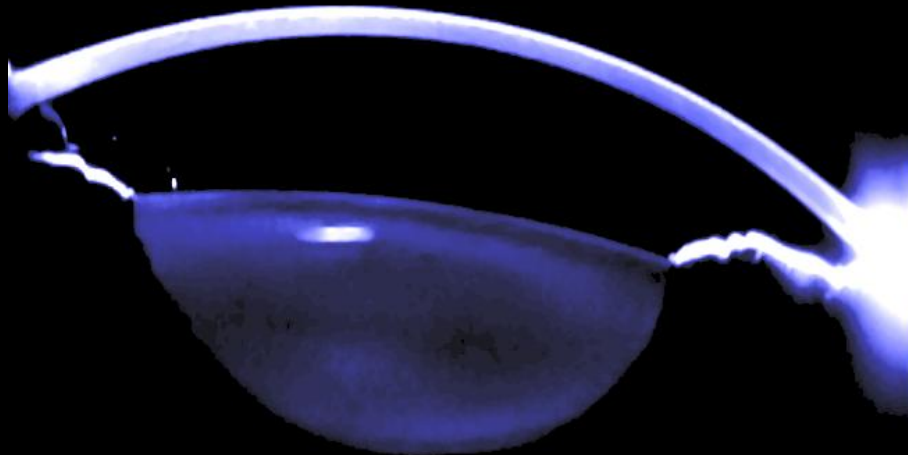


CONCLUSIONS

- The technique avoids extrapolating corneal data
- It overcomes the difficulty with the lack of symmetry of projected rings
- It provides a better description of the corneal morphology



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