Computational Design of Multiple Resonance–Type BN Molecules for Inverted Singlet and Triplet Excited States

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Abstract

A computational design of linearly extended multiple resonance (MR)-type BN molecules based on DABNA-1 is proposed herein in the quest to find potential candidates that exhibit a negative singlettriplet gap (ΔE_{ST}) and a large oscillator strength. The impact of a proper account of electron correlation in the lowest singlet and triplet excited states is systematically investigated by using double-hybrid functionals within the TD-DFT framework as well as wavefunction-based methods (EOM-CCSD and SCS-CC2) since this contribution plays an essential role in driving the magnitude of the ΔE_{ST} in MR-TADF and inverted singlet-triplet gap. Our results point out to a gradual reduction of the ΔE_{ST} gap with respect to the increasing sum of the number of B and N atoms, reaching negative ΔE_{ST} values for some molecules as a function of their size. The double hybrid functionals reproduce the gap with only slight deviation compared to available experimental data for DABNA-1, v-DABNA, and mDBCz and nicely agree with high-level quantum mechanical methods (e.g., EOM-CCSD and SCS-CC2). Larger oscillator strengths are found compared to the azaphenalene-type molecules also exhibiting the inversion of their singlet and triplet excited states. We hope this study can serve as a motivation for further design of the molecules showing negative ΔE_{ST} based on boron and nitrogen doped polyaromatic hydrocarbons.

Introduction

An excited state control of organic molecules is important for various light-related applications such as photocatalyst, phototherapy, bioimaging, organic light-emitting diodes, organic solar cells, etc. In closed shell (standard) molecules, the ground state is a singlet (S_0) state and the lower-lying excited singlet state (S_1) is typically a bright state that decays radiatively while the lowest excited

triplet state (T1) is a dark state that relaxes non-radiatively to S0 at room temperature before phosphorescence takes place due to the spin selection rule. In an organic light-emitting diode (OLED), these excited states are generated upon recombination of holes and electrons injected from the electrical contacts. However, the unfavorable spin statistics leads to 25% of emissive singlet excitons and 75% of non-emissive triplet excitons, besides potentially in a low internal quantum efficiency (IQE). Thermally activated delayed fluorescence (TADF)¹ and inverted singlet-triplet gap materials (INVEST)² have arisen as solutions to maximize IQE by bringing in near resonance S₁ and T₁ or T₁ above S₁. Therefore, intersystem crossing (ISC) and reverse intersystem crossing (rISC) processes between S₁ and T₁ states are important to control the relative population of both S₁ and T₁ excitons, with their rate largely affected by the energy difference between S₁ and T₁, i.e., $\Delta E_{ST} = E(S_1) - E(T_1)$. In the simpler picture of two interacting electrons occupying the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO), $E(T_1)$ is lower than $E(S_1)$ by twice the exchange interaction (K) of two electrons.³ The exchange interaction itself is by definition positive, so that it has been historically considered that ΔE_{ST} cannot be negative. However, it can be minimized by spatially separating the HOMO and LUMO orbitals to minimize orbital overlap. Such a strategy has been largely used in the TADF field.

In 1980, Leupin and Wirz reported that cyclazine, an azaphenalene molecule (molecule 1 in Figure S1) might show a negative ΔE_{ST} based on energy transfer experiments and the short lifetime (100 ns) recorded for T₁ state.⁴ More recently, Domcke *et al.* performed time-resolved photoluminescence spectroscopy on a heptazine derivative (molecule 2 in Figure S1), a core known previously for its TADF activity which did not exhibit the usual delayed fluorescence on the µs timescale. ⁵⁻⁸ They also performed transient absorption and did not detect any sign of the presence of triplet state. These two sets of experiments suggested that T₁ would lie higher in energy with respect to S₁ indicating a negative ΔE_{ST} gap that was further supported by sophisticated wave function-based quantum chemical calculations.⁸ Later on, researchers at RIKEN demonstrated experimentally that HzTFEX₂ (Figure S1), an heptazine derivative, exhibits a negative ΔE_{ST} , and consequently a krISC rate faster than kISC rate as estimated by temperature dependent transient photoluminescence spectroscopy.² As the INVEST has been mostly driven by the computational chemistry community, there have been many reports on theoretical and computational design of molecules showing negative ΔE_{ST} , but the molecular structures have been largely limited to the boron and/or nitrogen doped phenalene-type structures such as cyclazine and heptazine derivatives, ⁹⁻¹⁸ except a few reports of polyaromatic hydrocarbon cores (PAHs) compounds such as pentalene, COLDEM azulene-type alternant hydrocarbon molecule (compound **3** in Figure S1) is predicted to show a negative ΔE_{ST} .¹⁹⁻²²

With these precedents, it is easy to see that the expansion of the molecular design strategy (i.e., the search of new molecular cores and/or templates for further optimization with e.g. substituents) is not

only beneficial for establishing a dataset of possible candidates but is also interesting for the understanding of the underlying mechanism giving rise to a negative ΔE_{ST} . Two essential ingredients are mandatory to realize negative ΔE_{ST} : (i) the exchange interaction (K) should be as small as possible and (ii) electron correlation energy must stabilize S₁ more than 2·K. As consequence of (ii), the S₁ state wavefunction should contain a larger double excitation character than the T₁ state wavefunction as it has been recently emphasized in the literature. ^{14, 18} However, so far, INVEST compounds have shown only very small oscillator strengths and thus radiative decay rates which makes them prone to non-radiative decay and potentially reduced IQE.

How can we thus design new molecules with both a negative ΔE_{ST} and a large oscillator strength? Pershin *et al.* reported that electron correlation as accounted through double excitation contribution in wavefunction-based calculations, is key to rationalize the small ΔE_{ST} of the multi-resonance TADF (MR-TADF) DABNA-1. Their ΔE_{ST} is however still positive since its HOMO and LUMO orbitals exhibit some, yet small, overlap resulting in a non-negligible exchange energy. An additional feature of MR-TADF emitters in contrast to donor-acceptor TADF emitters is their consistently large oscillator strength because of the above-mentioned non-negligible HOMO-LUMO overlap.²³ Interestingly, Pershin *et al.* also reported that ΔE_{ST} of the boron- and nitrogen-incorporated MR molecules gradually reduces as its molecular structure is linearly extended while the oscillator strength increases.²⁴ Inspired by these previous reports, we considered that linearly extended MRtype chemical structures will be suitable candidates, potentially exhibiting with small exchange interaction in the excited state while the inherent electron correlation effect reported for this family of compounds could help realizing negative ΔE_{ST} concomitantly with large oscillator strength which would be relevant features for real devices and/or applications.

Taken all these findings together, we here computationally designed and proposed linearly extended MR-type BN molecules inspired by the seminal work on DABNA–1, showing negative ΔE_{ST} and large oscillator strength. This finding is the main novelty of this work as it differs considerably from the previously reported azaphenalene-like and heptazine structures displaying negative ΔE_{ST} but small oscillator strength due to the high symmetry of these cores. Double hybrid time-dependent density functional theory (TD–DFT) was used in the calculations to estimate ΔE_{ST} and oscillator strength. This class of methods represents a good trade-off between accuracy and computational cost.²⁵⁻²⁹ Wavefunction-based methods, such as the equation of motion coupled-cluster singles and doubles (EOM-CCSD) and the Spin-Component Scaling second-order approximate Coupled-Cluster (SCS-CC2), are considered for benchmarking ΔE_{ST} for smaller size systems.

Results and Discussion

Chemical structure of the linearly extended BN ladder-type molecules is shown in Figure 1. The

number of B and N atoms in their molecular composition is also reported in order to facilitate the comparison of the results. $E(S_1)$ and $E(T_1)$ energies, based on vertical excitation energies (i.e., $S_0 \rightarrow S_1$ and $S_0 \rightarrow T_1$), ΔE_{ST} , and oscillator strength associated with the $S_0 \rightarrow S_1$ transition of these ladder-type BN molecules are calculated with different methods and summarized in **Table 1**. The double hybrid TD-DFT with both B2PLYP and SOS-PBE-QIDH functionals give an expected smaller ΔE_{ST} than TD-DFT with B3LYP in all molecules, as a result from the inclusion of the double excitation contribution in double-hybrid functionals. ΔE_{ST} with any of the employed functionals gradually decreases upon increasing the molecular size to the point of becoming negative in the case of the double hybrid functionals. The most negative ΔE_{ST} value is estimated to be -0.086 eV for B9N9 system using SOS-PBE-QIDH functional. Basis set effects going from the cost-effective cc-pVDZ to cc-pVTZ were also evaluated using SOS-PBE-QIDH functional as the reference, resulting in negligible changes (e.g., differences for ΔE_{ST} less than 0.01 eV for B1N2, B2N1, B2N2, B2N3, and B3N2 taken as benchmark set) (**Table S1**). Based on these findings, the cc-pVDZ basis set is kept for the remaining calculations presented here, allowing the study of considerably large molecules.

As shown in **Figure S2a**, when ΔE_{ST} is plotted vs the number of π -electrons in the molecule, a clear decreasing trends appear, but some small opposite-trends also emerges periodically between the two molecules of which the sum of the number of B and N atoms are the same, for example, B1N2 and B2N1, B2N3 and B3N2, etc. This is rationalized because the contribution of N to the extension of π -conjugation is larger than the contribution of B due to the lone pair electrons in N. Therefore, the plot of ΔE_{ST} vs the sum of the number of B and N would not remove the small opposite-trends appearing in the plot (see **Figure S2b**); however, when ΔE_{ST} is plotted vs the sum of the number of B and half of the number of N (see **Figure 2**), the small periodical opposite-trends disappeared and the decreasing trend of ΔE_{ST} becoming much smoother. The curve fitting of ΔE_{ST} to the number of [B + N/2] using the inversely proportional formula y = a/x + b showed a high correlation with the R-squared (R²) values above 97% (**Table 2**). Extrapolated ΔE_{ST} values by the fitting are 0.091 eV from B3LYP, -0.113 eV from B2PLYP, and -0.138 eV from SOS-PBE-QIDH.

The experimental ΔE_{ST} value of B1N2 (DABNA-1) is reported to be 0.15 eV³⁰ and plotted as a black circle in **Figure 2**. The double-hybrid TD-DFT calculations showed much smaller error (small overestimation by 0.05–0.07 eV) for B1N2 to the experimental value than B3LYP does because of the poor account of electron correlation and are in line with the SCS-CC2 results which we demonstrated as method of choice for predicting ΔE_{ST} of MR-TADF materials with deviation in ΔE_{ST} of 0.03 and 0.06 eV for B2PLYP and SOS-PBE-QIDH, respectively. Among double-hybrid functionals tested on azaphenalene molecules, ²⁷⁻²⁹ SOS-PBE-QIDH has been reported as one of the most reliable functionals when predicting a negative ΔE_{ST} in this family of compounds. We also calculated two azaphenalene molecules synthesized by the RIKEN researchers reported to have

experimental ΔE_{ST} that amounts to -0.011 eV for HzTFEX₂ and 0.052 eV for HzPipX₂ (Table S2).² However, both double hybrid functionals, B2PLYP and SOS-PBE-QIDH, give overestimated negative ΔE_{ST} with errors with respect to the experiments ranging from -0.170 eV to -0.277 eV. Interestingly, neither EOM-CCSD nor SCS-CC2 methods are also able to predict a positive ΔE_{ST} for HzPipX₂ (Table S2). On the other hand, for comparison, we investigated the relatively large and actually synthesized BN-type molecule, v-DABNA and mDBCz, whose experimental ΔE_{ST} was reported to be as small as 0.017 eV³¹ and 0.040 eV³², respectively (**Table S2**). We obtained ΔE_{ST} of 0.057 eV from B2PLYP and 0.028 eV from SOS-PBE-QIDH for v-DABNA and ΔE_{ST} of 0.029 eV from B2PLYP and -0.118 eV from SOS-PBE-QIDH for mDBCz. Overall, we observed that B2PLYP leads to a good agreement with the experiments and SCS-CC2 calculations. We should remark that molecules larger than B1N2, among the calculated molecules in this study, remain predictions since they have not been synthesized so far. Interestingly, the longer BN ladder-type molecules follow the obtained decreasing trend toward negative ΔE_{ST} values as predicted by the double hybrid TD-DFT methods, mainly resulting from a decrease in the exchange energy. A proper account of correlation effect remains quite tricky so that the prediction of negative ΔE_{ST} should be cross-compared between different computational methods. However as mentioned above, wavefunction-based methods are not accessible for the full range of systems, therefore we must also consider the possibility that the computationally predicted negative ΔE_{ST} of the BN ladder-type molecules would lie within the error bar of the methods possibly resulting in an actual slightly positive ΔE_{ST} . Likely, we expect that the magnitude of the error would not be systematic and would depend on the systems size. Still, if we consider the error obtained for the ΔE_{ST} of DABNA-1 with the B2PLYP and SOS-PBE-QIDH doublehybrid functionals, B9N9 would thus result in a positive ΔE_{ST} .

To summarize briefly, the double hybrid TD-DFT calculations lead to the following results: 1) ΔE_{ST} was underestimated for the azaphenalene molecules, HzTFEX₂ and HzPipX₂, by an error from -0.170 eV to -0.277 eV; 2) ΔE_{ST} was overestimated for the BN molecules, DABNA-1 and v-DABNA, by the error from 0.011 eV to 0.072 eV, and underestimated for mDBCz by the error from -0.011 eV to -0.158 eV. We still cannot rule out the possibility that the quality of the double-hybrid functional largely depends on the type and/or size of molecules due to the lack of experimental data on related molecules. Additionally, we can neither rule out the influence of dynamic and/or polarization effects³³ on the experimental values, which could further influence the comparison between theoretical and experimental results.

Perusing into the results obtained by double-hybrid functionals, the perturbative correction (D) of the S_1 state is as expected larger than that of T_1 state, or in other words, the double excitations contribution is more pronounced in the S_1 than in the T_1 state (**Figure 3**). The (D) values for the S_1 state obtained with B2PLYP and SOS-PBE-QIDH are very similar, but for the T_1 state, SOS-PBE- QIDH showed smaller (D) values than B2PLYP. The (D) correction in the S₁ state, is less dependent on the extension of π -conjugation than for the T₁ state. Furthermore, the (D) correction in the S₁ state is minimized for B3N3 and slightly increases for longer compounds. A potential explanation could be that the S₁ electronic density is so spread upon the extension of π -conjugation that the correlation effects are slightly weaker. Besides, the (D) value of the T₁ state gradually becomes more negative with the extension of π -conjugation, and approaches a constant value, indicating that even T₁ can have a certain double excitation character with increasing the π -conjugation. The constant value of the T₁ (D) value might arise from the stronger localization of the triplet state in comparison to S₁.

Oscillator strengths (*f*) increase with the extension of π -conjugation, and the sum of the number of B and half of the number of N also shows a better correlation than the number of π -electrons (**Figure S3**). The increase of oscillator strength with the extension of π -conjugation can be attributed to increase of polarizability in the extended systems. This is very much in line with the work of Vezie et al. that reported that the oscillator strength of several π -conjugated oligomers normalized by the number of π -electrons in the system increases due to the superlinear increase of the polarizability with the increase of the number of π -electrons. ³⁴ The BN molecules in this study also exhibit a same trend (**Figure 4**), since the transition dipole moment of the S₁ state is aligned with the long axis of the molecules. Consequently, relative large oscillator strength values can be achieved concomitantly with negative ΔE_{ST} . This is a finding totally different from the previously reported negative ΔE_{ST} compounds, such as azaphenalene and fused alternant hydrocarbons^{8, 9, 17}, and could pave the way towards reliable devices and/or further applications.

In addition to the linearly extended BN molecules, the ΔE_{ST} and the oscillator strengths of a set of topologically different (zigzag-, circulene-, and graphene-type) BN molecules were also calculated with double-hybrid TD-DFT methods (**Figure 5** and **Table 3**). The zigzag-type BN molecules also showed negative ΔE_{ST} and large oscillator strength. In addition, we predicted largely negative ΔE_{ST} for circulene- and graphene-type molecules that amounts to -0.153 eV for B9N9_C and -0.269 eV for B12N12_G with the SOS-PBE-QIDH functional, but their oscillation strength is zero likely originating from the high symmetry point group of these compounds.

Conclusions

We designed a large set of linearly extended MR-type BN molecules inspired by the DABNA–1 MR-TADF emitter, which computationally showed negative ΔE_{ST} and large oscillator strength, based on B2PLYP and SOS-PBE-QIDH double-hybrid functionals calculations that are able to introduce electron correlation effect into excited-states of any multiplicity through a second-order perturbative correction. The gradual decrease of ΔE_{ST} to achieve a negative ΔE_{ST} value displayed a high correlation with the increasing sum of the number of B and half N atoms in the molecular structure, which is a key result for the molecular design strategy. The double-hybrid functionals selected reproduced the experimental ΔE_{ST} of DABNA-1, v-DABNA, and mDBCz with only slight deviations and provide a good agreement with more robust wavefunction-based approaches (EOM-CCSD and SCS-CC2). Nonetheless, we still cannot deny the possibility that these methods overestimated ΔE_{ST} (i.e., predicted to be too negative) of the most extended BN molecules. It is extremely hard to actually synthesize the extended BN molecules, so that the verification of the negative ΔE_{ST} is now pending. Another key result is that these extended BN molecules, while showing negative ΔE_{ST} values, display relatively large oscillator strengths in contrast to the azaphenalene molecules that were identified as INVEST materials. Finally, the molecular design followed in this study will help to widen the set of molecules for which a negative ΔE_{ST} is predicted, and to consequently develop INVEST emitter with a high radiative decay rate molecules efficient triplet-harvesting abilities for OLED applications.

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Figure 1. Chemical structures of the ladder-type BN molecules.



Figure 2. ΔE_{ST} plotted vs sum of the number of B and half N. The black circle represents the experimental ΔE_{ST} of B1N2 (DABNA-1) as 0.15 eV. The dotted lines are a curve fitting line.



Figure 3. Double-hybrid functional perturbative correction (D) as a function of the sum of the number of B and half of N.



Figure 4. Oscillator strength computed at the TD-DFT level normalized by the number of π -electrons as a function of the sum of the number of B and half of N.

N(e) ^{b)} B+N ^{c)} B+N/2 ^{d)}					B3L	YP ^{a)}			B2P	LYP ^{a)}		SOS-PBE-QIDH ^{a)}				
	$N(e)^{6/3}B+N^{6/3}B+N/2^{6/3}$			$E(S_1)^{e)}$	f/N ^{f)}	$E(T_1)^{e)}$	ΔE_{ST}	$E(S_1)^{e)}$	$f/N^{f)}$	$E(T_1)^{e)}$	ΔE_{ST}	$E(S_1)^{e)}$	f/N ^{f)}	$E(T_1)^{e)}$	ΔE_{ST}	
B1N2	34	3	2.0	3.083	0.0058	2.598	0.484	2.753	0.0078	2.556	0.197	3.245	0.0111	3.023	0.222	
B2N1	32	3	2.5	2.955	0.0077	2.504	0.450	2.601	0.0091	2.433	0.168	3.111	0.0120	2.980	0.131	
B2N2	40	4	3.0	2.729	0.0083	2.308	0.421	2.361	0.0099	2.229	0.132	2.925	0.0135	2.816	0.109	
B2N3	48	5	3.6	2.610	0.0087	2.249	0.361	2.233	0.0099	2.149	0.084	2.811	0.0137	2.747	0.064	
B3N2	46	5	4.0	2.599	0.0101	2.276	0.323	2.215	0.0114	2.159	0.056	2.810	0.0157	2.810	0.000	
B3N3	54	6	4.5	2.494	0.0095	2.203	0.292	2.110	0.0111	2.078	0.032	2.736	0.0159	2.741	-0.005	
B3N4	62	7	5.0	2.375	0.0099	2.100	0.276	1.982	0.0107	1.956	0.026	2.598	0.0152	2.591	0.007	
B4N3	60	7	5.5	2.405	0.0115	2.145	0.261	2.018	0.0124	2.009	0.009	2.636	0.0174	2.670	-0.034	
B4N4	68	8	6.0	2.321	0.0104	2.080	0.241	1.932	0.0115	1.933	-0.001	2.569	0.0165	2.596	-0.027	
B4N5	76	9	6.5	2.274	0.0109	2.047	0.227	1.882	0.0115	1.891	-0.009	2.515	0.0166	2.538	-0.023	
B5N4	- 74	9	7.0	2.300	0.0122	2.077	0.223	1.912	0.0129	1.927	-0.015	2.541	0.0182	2.583	-0.042	
B5N5	81	10	7.5	2.245	0.0112	2.039	0.206	1.859	0.0122	1.883	-0.024	2.504	0.0177	2.544	-0.040	
B5N6	90	11	8.0	2.217	0.0117	2.021	0.195	1.830	0.0122	1.860	-0.030	2.470	0.0177	2.514	-0.044	
B6N5	88	11	8.5	2.220	0.0131	2.031	0.190	1.836	0.0137	1.872	-0.036	2.471	0.0196	2.524	-0.053	
B6N6	96	12	9.0	2.197	0.0123	2.017	0.181	1.817	0.0131	1.857	-0.040	2.457	0.0190	2.512	-0.055	
B6N7	104	13	9.5	2.182	0.0123	2.008	0.174	1.799	0.0128	1.845	-0.046	2.441	0.0184	2.501	-0.060	
B7N6	102	13	10.0	2.198	0.0133	2.024	0.174	1.815	0.0136	1.862	-0.047	2.454	0.0194	2.519	-0.065	
B7N7	110	14	10.5	2.172	0.0130	2.008	0.164	1.793	0.0135	1.846	-0.053	2.434	0.0194	2.502	-0.068	
B9N9	138	18	13.5	2.134	0.0136	1.995	0.139	1.759	0.0138	1.829	-0.070	2.402	0.0198	2.488	-0.086	

Table 1. Vertical excitation energies (eV), oscillator strength (f) , and ΔE_{ST} of the ladder-type BN molecules, as calculated with different methods.

a) With the cc-pVDZ basis set. b) The number of π -electrons. c) Sum of the number of B atoms and the number of N atoms. d) Sum of the number of B atoms and half the number of N atoms. e) Vertical excitation energy at $S_0 \rightarrow S_1$ and $S_0 \rightarrow T_1$. f) Oscillator strength normalized by the number of π -electrons associated with the $S_0 \rightarrow S_1$ transition.

Table 2. ΔE_{ST} (eV) value obtained by extrapolation of the fitting curve and coefficient of determination.

	π-elec	trons	B	+ N	B + N/2		
	ΔE_{ST}	\mathbb{R}^2	ΔE_{ST}	\mathbb{R}^2	ΔE_{ST}	\mathbb{R}^2	
B3LYP	0.031	0.9767	0.087	0.9760	0.091	0.9734	
B2PLYP	-0.157	0.9712	-0.116	0.9857	-0.113	0.9868	
SOS-PBE-QIDH	-0.175	0.8735	-0.138	0.9238	-0.138	0.9739	



Figure 5. Chemical structure of the zigzag-, circulene-, and graphene-type BN molecules.

	$N(a)^{b}$ $B+N^{c}$ $B+N^{1/2d}$				B3L	YP ^{a)}			B2PI	LYP ^{a)}		SOS-PBE-QIDH ^{a)}				
	N(e)	DTIN-	[,] D ⊤I N /∠ ^{-,}	$S_1 \leftarrow S_0^{e}$	f/N ^{f)}	$T_1 \leftarrow S_0^e$	ΔE_{ST}	$S_1 \leftarrow S_0^{e}$	f/N ^{f)}	$T_1 \leftarrow S_0^{e}$	ΔE_{ST}	$S_1 \leftarrow S_0^{e}$	f/N ^{f)}	$T_1 \leftarrow S_0^{e}$) ΔE_{ST}	
B4N4_Z	68	8	6	2.327	0.0073	2.103	0.224	1.970	0.0106	1.995	-0.025	2.650	0.0166	2.674	-0.024	
B5N5_Z	82	10	7.5	2.269	0.0073	2.089	0.180	1.931	0.0120	1.984	-0.053	2.623	0.0188	2.678	-0.055	
B6N6_Z	96	12	9	2.238	0.0071	2.085	0.154	1.918	0.0131	1.982	-0.064	2.603	0.0201	2.676	-0.073	
B7N7_Z	110	14	10.5	2.225	0.0068	2.087	0.138	1.915	0.0137	1.984	-0.069	2.590	0.0204	2.676	-0.086	
B3N3_C	48	6	4.5	2.975	0.0000	2.643	0.331	2.611	0.0000	2.706	-0.095	3.139	0.0000	3.248	-0.109	
B9N9_C	126	18	13.5	2.054	0.0000	1.946	0.108	1.705	0.0000	1.819	-0.114	2.331	0.0000	2.484	-0.153	
B12N12_C	6 138	24	18	2.411	0.0000	2.264	0.146	1.993	0.0000	2.150	-0.157	2.715	0.0000	2.984	-0.269	

Table 3. Vertical excitation energies (eV), oscillator strength, and ΔE_{ST} values of the zigzag- and circulene-type BN molecules, as calculated with different methods.

a) With the cc-pVDZ basis set. b) The number of π -electrons. c) Sum of the number of B atoms and the number of N atoms. d) Sum of the number of B atoms and half the number of N atoms. e) Vertical excitation energy at $S_0 \rightarrow S_1$ and $S_0 \rightarrow T_1$. f) Oscillator strength normalized by the number of π -electrons associated with the $S_0 \rightarrow S_1$ transition.

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Supporting Information

Methodology

All ground-state molecular structures were optimized at the B3LYP/cc-pVDZ level and showed positive frequencies. First estimate of the excitation energies at the same level was performed with employing Time-Dependent Density-Functional Theory (TD-DFT). TD-DFT with the B2PLYP^{1, 2} and SOS-PBE-QIDH³ double hybrid functionals was also employed since it considers electron correlation and double excitation effects in its implementation. These expressions incorporate the electron correlation effect by adding a second-order Møller–Plesset perturbation theory (MP2) contribution to Hartree-Fock (HF) exchange and standard generalized gradient approximations (GGAs) for exchange and for correlation, as for the B2PLYP case.

$$E_{\rm XC}{}^{\rm B2PLYP} = c_x E_{\rm X}{}^{\rm HF} + (1 - c_x) E_{\rm X}{}^{\rm B88\,GGA} + (1 - c_c) E_{\rm C}{}^{\rm LYP\,GGA} + c_c E_{\rm C}{}^{\rm MP2}$$
(1)

 ΔE_{ST} can be then estimated by computing the corresponding vertical excitation energies that can be formally written as the sum of the conventional TD-DFT and configuration interaction singles with perturbative doubles (CIS(D)) corrections, with the latter term responsible for taking into account the electron correlation effect, corresponding to the ground state MP2 correction.

$$\Delta E^{\text{B2PLYP}}(c_x, c_c) = \Delta E^{\text{TD-DFT}}(c_x, c_c) + c_c \Delta E^{\text{CIS(D)}}$$
(2)

Originally, weights of 0.53 and 0.27 have been used for c_x and c_c , respectively, for the B2PLYP functional. Recently, Kondo reported that 0.40 for c_x gave a closer ΔE_{ST} for DABNA-1 to its experimental value, while c_c remained at its original value of 0.27.⁴ In this study, the set $(c_x, c_c) = (0.40, 0.27)$ was used for B2PLYP functional to allow comparison with previously reported results in literature for DABNA-1.

SOS-PBE-QIDH is a spin-opposite-scaled (SOS) version of the quadratic integrand double-hybrid (QIDH) functional that also incorporates as ingredients HF and PBE exchange, as well as MP2 and PBE correlation, using the following expression:

$$E_{\rm XC}^{\rm PBE-QIDH} = [(\lambda + 2)/3]E_{\rm X}^{\rm HF} + [(1 - \lambda)/3]E_{\rm X}^{\rm PBE\,GGA} + (2/3)E_{\rm C}^{\rm PBE\,GGA} + (1/3)E_{\rm C}^{\rm MP2}$$
(3)

with $\lambda = 3^{2/3} - 2.5$

In the vertical excitation energies calculation, $E_C^{CIS(D)}$ is separated into direct and indirect terms as follows:

$$E^{\text{CIS}(D)} = \langle \Phi_{\text{CIS}} | \hat{V} | \hat{U}_2 \Phi_0 \rangle + \langle \Phi_{\text{CIS}} | \hat{V} | \hat{T}_2 \hat{U}_1 \Phi_0 \rangle \tag{4}$$

where \hat{U}_2 and \hat{U}_1 are the operators generating the doubly and singly excited wave functions from the HF determinant (Φ_0), respectively. \hat{T}_2 is the operator generating the double excitation of two inactive electrons, \hat{V} is a perturbation potential, and Φ_{CIS} is the CIS wave function. The electron pair contributions in the excitation can be divided into opposite-spin (OS) and same-spin (SS) contributions to be weighed differently. The two terms in equation (4) are broken down into opposite-and same-spin components.

$$E^{\text{CIS}(D)} = \langle \Phi_{\text{CIS}} | \hat{V} | (C_U^{\text{OS}} \hat{U}_2 + C_U^{\text{SS}} \hat{U}_2) \Phi_0 \rangle + \langle \Phi_{\text{CIS}} | \hat{V} | (C_T^{\text{OS}} \hat{T}_2 + C_T^{\text{SS}} \hat{T}_2) \hat{U}_1 \Phi_0 \rangle$$
(5)

where C_U^{OS} and C_U^{SS} are, respectively, the opposite- and same-spin scale parameters for the direct term, and C_T^{OS} and C_T^{SS} are, respectively, the related parameters for the indirect term. By setting the same-spin scale parameters to zero, i.e., $C_U^{SS} = 0$ and $C_T^{SS} = 0$, one recovers the original SOS-CIS(D) method.

$$E^{\text{SOS-CIS}(D)} = \langle \Phi_{\text{CIS}} | \hat{V} | C_{\text{U}}^{\text{OS}} \hat{U}_2 \Phi_0 \rangle + \langle \Phi_{\text{CIS}} | \hat{V} | C_{\text{T}}^{\text{OS}} \hat{T}_2 \hat{U}_1 \Phi_0 \rangle$$
(6)

However, for the SOS-PBE-QIDH case, $C_T^{OS} = 0.5470$ and $C_U^{OS} = 0.5730$ are obtained by fitting to excited-state datasets and will be thus used also here.

As reference and sanity check, equation-of-motion coupled-cluster singles and doubles (EOM-CCSD) and second-order approximate coupled cluster singles and doubles with the spin-component scaled correction (SCS-CC2) approaches were also employed for some of the smallest systems. EOM-CCSD calculations were done with Q-Chem 5.3.0, ⁶ while SCS-CC2 calculations were performed with TURBOMOLE 7.5.⁷ Double hybrid TD-DFT calculations with B2PLYP and SOS-PBE-QIDH were performed with ORCA 5.0.3. ⁸ TD-DFT calculation with B3LYP was performed with Gaussian 16 RevC.01. All these calculations were carried out using the double-zeta dunning basis set (cc-pVDZ).⁹







HzTFEX₂

HzPipX₂



v-DABNA mDBCz

Figure S1. Chemical structures of the previously reported compounds.

1 **Table S1**. Vertical excitation energies (eV) and ΔE_{ST} of B1N2, B2N1, B2N2, B2N3, B3N2 with the cc-pVTZ basis set

	SOS-PBE-QIDH												
	$E(S_1)^{a)}$	$E(T_1)^{a)}$	ΔE_{ST}										
B1N2	3.196	2.983	0.213										
B2N1	3.078	2.947	0.131										
B2N2	2.891	2.785	0.106										
B2N3	2.774	2.713	0.061										
B3N2	2.780	2.773	0.007										

2 a) Vertical excitation energy at $S_0 \rightarrow S_1$ and $S_0 \rightarrow T_1$.

3

4

5 Table S2. Vertical excitation energies (eV), oscillator strength (f), and ΔE_{ST} of smaller size molecules at the EOM-CCSD and SCS-CC2 levels of theory.

	exp	EOM-CCSD ^{a)}			SCS-CC2 ^{a)}				B2PLYP				SOS-PBE-QIDH				
	ΔE_{ST}	$E(S_1)^{b)}$	f ^{c)}	$E(T_1)^{b}$	ΔE_{ST}	$E(S_1)^{b)}$	f ^{c)}	$E(T_1)^{b}$	ΔE_{ST}	$E(S_1)^{b)}$	f ^{c)}	$E(T_1)^{b)}$	ΔE_{ST}	$E(S_1)^{b)}$	f ^{c)}	$E(T_1)^{b}$	ΔE_{ST}
HzTFEX ₂	-0.011	3.136	0.021	3.252	-0.116	3.039	0.024	3.382	-0.285	2.579	0.028	2.855	-0.276	2.964	0.045	3.252	-0.288
$HzPipX_2$	0.052	3.248	0.037	3.307	-0.059	3.142	0.040	3.427	-0.343	2.664	0.039	2.782	-0.118	3.060	0.062	3.258	-0.198
B1N2 (DABNA-1)	0.150	3.448	0.334	3.110	0.338	3.294	0.308	3.129	0.165	2.753	0.264	2.556	0.197	3.245	0.376	3.023	0.222
mDBCz	0.040				n/a	2.792	0.742	2.753	0.039	2.050	0.582	2.021	0.029	2.636	0.802	2.754	-0.118
v-DABNA	0.017				n/a	3.095	0.701	3.076	0.019	2.482	0.657	2.425	0.057	3.046	0.778	3.018	0.028

6 a) With the cc-pVDZ basis set. b) Vertical excitation energy at $S_0 \rightarrow S_1$ and $S_0 \rightarrow T_1$. c) Oscillator strength associated with the $S_0 \rightarrow S_1$ transition.

7



Figure S2. ΔE_{ST} plotted vs a) the number of π -electrons, and b) the number of B and N. The dotted lines are a curve fitting line.

13

8 10

14 15



16 Figure S3. Oscillation strength vs a) the number of π -electrons and b) sum of the number of B and

- 17 half of N.
- 18

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